

* a "library" of RNNs

dx

dy

mag

ori

ori hist

shift image (dx, dy)

translational symmetry

point symmetry (corners)

FEP

rotation symmetry

perception classifier — learns

* composition mechanism

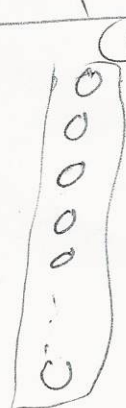
* execution capability

* set of text images + ground truth

see $\begin{pmatrix} 12 \times 11 \\ 3 \times 15 \times 15 \end{pmatrix}$ NOTES/Tanya/chars

* classification experiments

library inputs



Library Model (RNN) set

~~name~~

RNN(i).name = 'dx'

RNN(i).W = W

RNN(i).f = f-vector = $\begin{bmatrix} f_1 \\ f_2 \\ \vdots \end{bmatrix}$

RNN(i).u0 = initial vector
inputs + outputs 0

RNN(i).I = $[I_1, I_2, \dots, I_m]$

RNN(i).O = $[O_1, O_2, \dots, O_n]$

RNN(i).uf = $\bar{u}_f$

num. ~~steps~~
steps

no change

type = 'program'
'input'

Execution Model

interface funcln
out = TA-run-RNN(input_name,
RNN_name,
Library ~~ids~~),

input:

weight matrix, $W: n \times n$ array

function at each node, f_i

input ~~neurons~~ (identify) m values

input ~~neurons~~ $I = \{I_1, \dots, I_m\}$ $I_i \in \{1, 2, \dots, n\}$

initial configuration, $\bar{u}_0$

end of computation configuration or max steps $\bar{u}_f$

output neurons (identify) $O = \{O_1, O_2, \dots, O_k\}$
 $O_i \in \{1, 2, \dots, n\}$

execution

$$\bar{u}_{t+1} = W \bar{u}_t$$

$$\bar{u}_{t+1} = \bar{f}(\bar{u}_{t+1}) \equiv \bigoplus_i [f_i(u_{t+1}, i)]$$

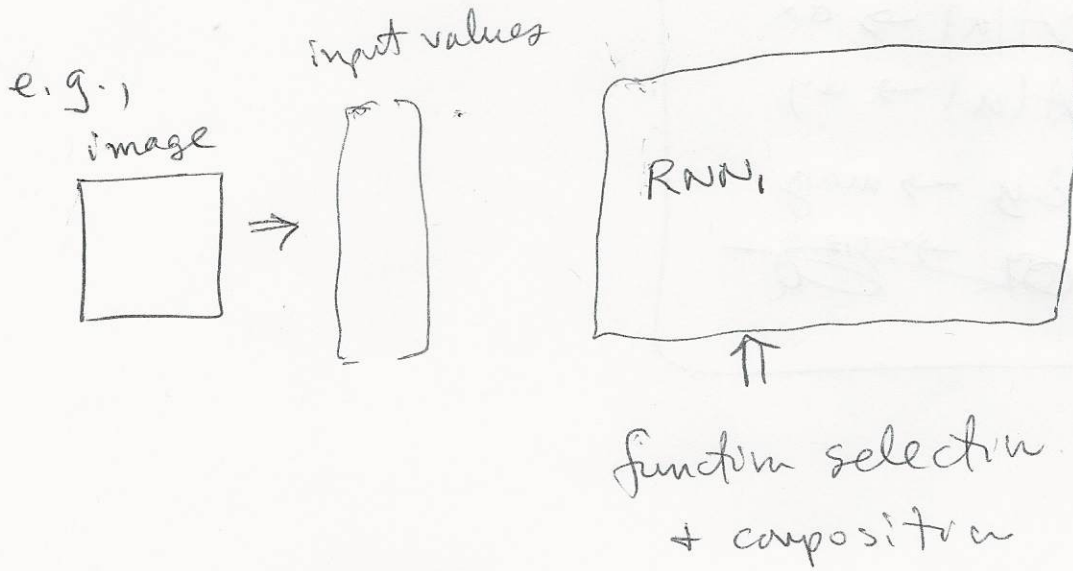
$$\text{till } \bar{u}_{t^*} = \bar{u}_f$$

output

values of ~~neurons~~ $[u_{f, O_1}, \dots, u_{f, O_k}]$

~~given~~

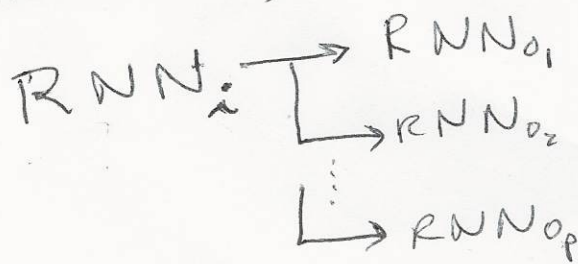
Composition Mechanism



$\rightarrow$ RNN $\rightarrow$

input RNN
RNN

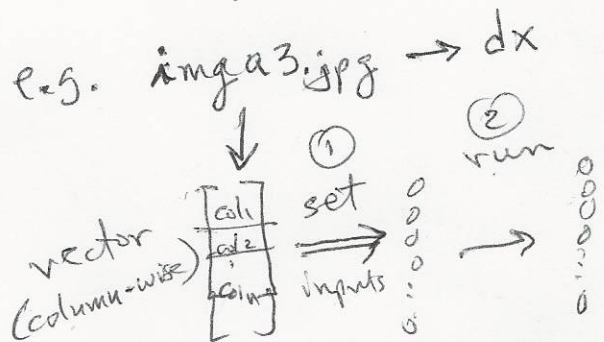
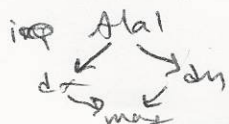
connectivity



input special name

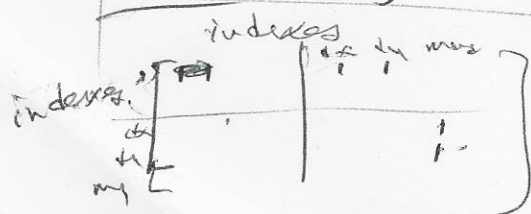
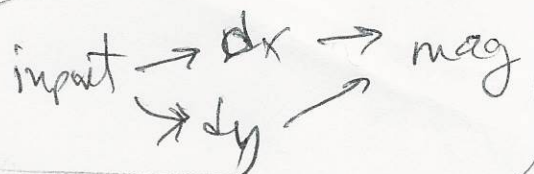
input $\rightarrow$ RNN

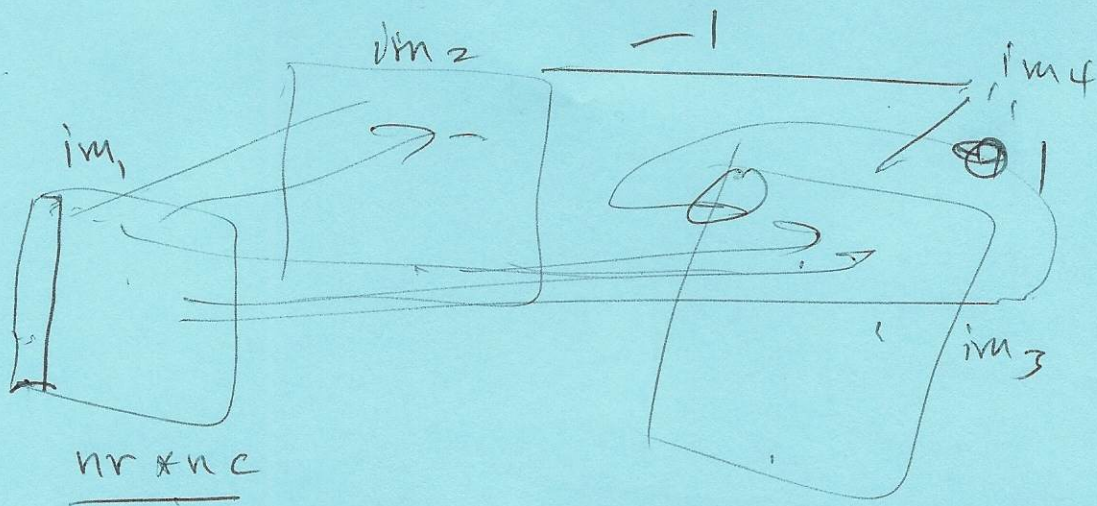
(Ala) $\rightarrow$ {dx, dy} $\rightarrow$ mag



static vs. dynamic input

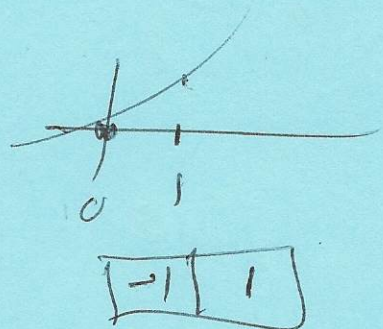
$\rightarrow$ assume static for our problem



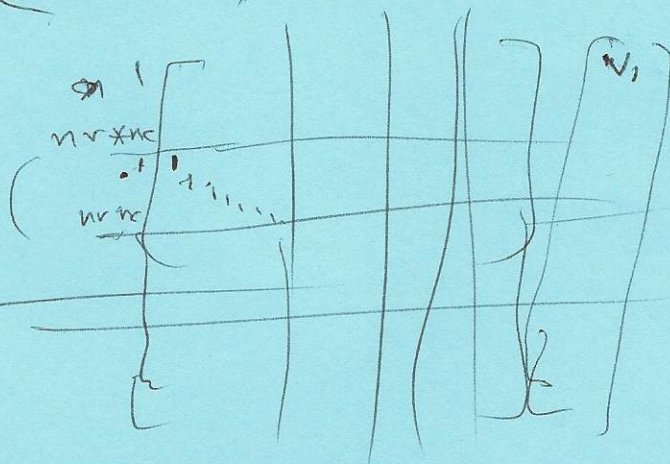


$$\text{func RNN} = \text{TA-dx-RNN}(nr, nc)$$

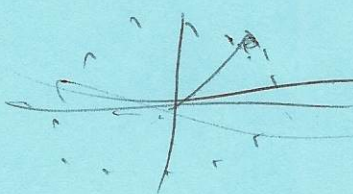
$$\begin{aligned} \text{lim 2} &\leftarrow \text{lim 1} \\ \text{lim 3}(\text{index}(1,1)) &\leftarrow \text{lim 1}(\text{index}(1,1)) \end{aligned}$$



$$\text{lim 4}(\text{index}(1,1)) \leftarrow \text{lim 2}(\text{index}(1,1)) - \text{lim 3}(\text{index}(1,1))$$



W further identity



$$\begin{aligned} &0 + 2 \\ &-1 \ 0 \ 1 \ dx \\ &-1 \ 0 \ 1 \ dy \end{aligned}$$