Computation versus Programming

• Last time, we talked about computation



• Programming?



We somehow wrote the function in one big, creative chunk

Design Recipe I

Data

• Understand the input data: num, bool, sym, or image

Contract, Purpose, and Header

• Describe (but don't write) the function

Examples

• Show what will happen when the function is done

Body

• The most creative step: implement the function body

Test

• Run the examples

Data

Choose a representation suitable for the function input

- Fahrenheit degrees 🐤 num
- Grocery items 🔶 sym
- Faces 🔶 image
- Wages 🔸 num
- ...

Handin artifact: none for now

Contract, Purpose, and Header

Contract

Describes input(s) and output data

- f2c : num -> num
- is-milk? : sym -> bool
- wearing-glasses? : image image image -> bool
- netpay : num -> num

Handin artifact: a comment

; f2c : num -> num
; is-milk? : sym -> bool

Contract, Purpose, and Header

Purpose

Describes, in English, what the function will do

- Converts F-degrees **f** to C-degrees
- Checks whether **s** is a symbol for milk
- Checks whether **p2** is **p1** wearing glasses **g**
- Computes net pay (less taxes) for **n** hours worked

Handin artifact: a comment after the contract

- ; f2c : num -> num
- ; Converts F-degrees f to C-degrees

Contract, Purpose, and Header

Header

Starts the function using variables that are metioned in purpose

- (define (f2c f))
- (define (is-milk? s))
- (define (wearing-glasses? p1 p2 g))
- (define (netpay n))

Check: function name and variable count match contract

Handin artifact: as above, but absorbed into implementation

; f2c : num -> num
; Converts F-degrees f to C-degrees
(define (f2c f))

Examples

Show example function calls an result

```
(f2c 32) "should be" 0
(f2c 212) "should be" 100
```

```
(is-milk? 'milk) "should be" true
(is-milk? 'apple) "should be" false
```

Check: function name, argument count and types match contract

Handin artifact: as above, after header/body

```
; f2c : num -> num
; Converts F-degrees f to C-degrees
(define (f2c f) ...)
(f2c 32) "should be" 0
(f2c 212) "should be" 100
```

Body

Fill in the body under the header

(define (f2c f) (* (- f 32) 5/9)) (define (is-milk? s) (symbol=? s 'milk))

Handin artifact: complete at this point

; f2c : num -> num
; Converts F-degrees f to C-degrees
(define (f2c f)
 (* (- f 32) 5/9))
(f2c 32) "should be" 0
(f2c 212) "should be" 100

Compound Data Design Recipe - Each Step Has a Purpose Data A posn is • Shape of input data will drive the implementation (make-posn num num) **Contract, Purpose, and Header** • (make-posn 1 2) is a value • Provides a first-level understanding of the function • (posn-x (make-posn 1 2)) \rightarrow 1 Examples • (posn-y (make-posn 1 2)) \rightarrow 2 • Gives a deeper understanding and exposes specification issues Body How about program design? • The implementation is the whole point Test Evidence that it works

Body

If the input is compound data, start the body by selecting the parts

```
; max-part : posn -> num
; Return the X part of p is it's bigger
; than the Y part, otherwise the Y part
(define (max-part p)
   ...)
```

(max-part (make-posn 10 11)) "should be" 11
(max-part (make-posn 7 5)) "should be" 7

Body

If the input is compound data, start the body by selecting the parts

; max-part : posn -> num ; Return the X part of p is it's bigger ; than the Y part, otherwise the Y part (define (max-part p) ... (posn-x p) ... (posn-y p) ...)

(max-part (make-posn 10 11)) "should be" 11 (max-part (make-posn 7 5)) "should be" 7

Body

If the input is compound data, start the body by selecting the parts

```
; max-part : posn -> num
; Return the X part of p is it's bigger
; than the Y part, otherwise the Y part
(define (max-part p)
  (cond
    [(> (posn-x p) (posn-y p)) (posn-x p)]
    [else (posn-y p)]))
(max-part (make-posn 10 11)) "should be" 11
(max-part (make-posn 7 5)) "should be" 7
```

Body

If the input is compound data, start the body by selecting the parts

```
; max-part : posn -> num
; Return the X part of p is it's bigger
; than the Y part, otherwise the Y part
(define (max-part p)
  (cond
    [(> (posn-x p) (posn-y p)) (posn-x p)]
    [else (posn-y p)]))
(max-part (make-posn 10 11)) "should be" 11
(max-part (make-posn 7 5)) "should be" 7
```

Since this guideline applies before the usual body work, let's split it into an explicit step

Design Recipe II

Data

• Understand the input data

Contract, Purpose, and Header

• Describe (but don't write) the function

Examples

• Show what will happen when the function is done

Template

• Set up the body based on the input data (and only the input)

Body

• The most creative step: implement the function body

Test

• Run the examples

Body Template

If the input is compound data, start the body by selecting the parts

```
; max-part : posn -> num
; ...
(define (max-part p)
    ... (posn-x p) ... (posn-y p) ...)
```

Check: number of parts in template = number of parts data definition named in contract

A posn is

(make-posn num num)

Body Template

Data

If the input is compound data, start the body by selecting the parts

Handin artifact: a comment (required starting with HW 3)

```
; max-part : posn -> num
; Return the X part of p is it's bigger
; than the Y part, otherwise the Y part
; (define (max-part p)
; ... (posn-x p) ... (posn-y p) ...)
(define (max-part p)
 ... (posn-x p) ... (posn-y p) ...)
(max-part (make-posn 10 11)) "should be" 11
(max-part (make-posn 7 5)) "should be" 7
```

Here's what we'd like: A snake is (make-snake sym num sym) We can tell DrScheme about snake: (define-struct snake (name weight food)) Creates the following: • make-snake • snake-name • snake-weight • snake-food **Expanding the Zoo** We have snakes, and armadillos are similar. Let's add ants. An ant has • a weight a location in the zoo

```
Now that we've defined snake, we can use it in contracts
```

Deciding to define **snake** is in the first step of the design recipe

(make-snake sym num sym)

(define-struct snake (name weight food))

Handin artifact: a comment and/or define-struct

; A snake is

; An ant is
; (make-ant num posn)
(define-struct ant (weight loc))

(make-ant 0.001 (make-posn 4 5))

(make-ant 0.007 (make-posn 3 17))

Programming with Ants

• Define **ant-at-home?**, which takes an ant and reports whether it is at the origin

Programming with Ants

Contract, Purpose, and Header

; ant-at-home? : ant -> bool

Programming with Ants

Contract, Purpose, and Header

- ; ant-at-home? : ant -> bool
- ; Check whether ant a is home

Programming with Ants

Contract, Purpose, and Header

Programming with Ants

Programming with Ants



```
; ant-at-home? : ant -> bool
; Check whether ant a is home
(define (ant-at-home? a)
        ...)
```

```
Template
; ant-at-home? : ant -> bool
; Check whether ant a is home
(define (ant-at-home? a)
    ... (ant-weight a)
```

... (ant-loc a) ...)

(ant-at-home? (make-ant 0.001 (make-posn 0 0))) '= true (ant-at-home? (make-ant 0.001 (make-posn 1 1))) '= false (ant-at-home? (make-ant 0.001 (make-posn 0 0))) '= true (ant-at-home? (make-ant 0.001 (make-posn 1 1))) '= false

Programming with Ants

Template

```
; ant-at-home? : ant -> bool
; Check whether ant a is home
(define (ant-at-home? a)
   ... (ant-weight a)
```

```
... (posn-at-home? (ant-loc a)) ...)
```

New template rule: data-defn reference \Rightarrow template reference

Add templates for referenced data, if needed, and implement body for referenced data

```
(ant-at-home? (make-ant 0.001 (make-posn 0 0))) '= true
(ant-at-home? (make-ant 0.001 (make-posn 1 1))) '= false
```

Programming with Ants

Template

```
; ant-at-home? : ant -> bool
```

```
; Check whether ant a is home
```

```
(define (ant-at-home? a)
```

```
... (ant-weight a)
```

```
... (posn-at-home? (ant-loc a)) ...)
```

```
(define (posn-at-home? p)
... (posn-x p) ... (posn-y p) ...)
```

(ant-at-home? (make-ant 0.001 (make-posn 0 0))) '= true (ant-at-home? (make-ant 0.001 (make-posn 1 1))) '= false

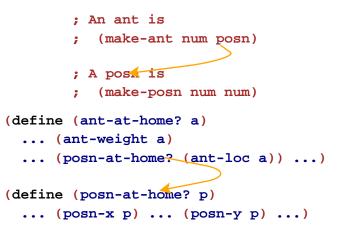
Programming with Ants

Shapes of Data and Templates

Body

```
; ant-at-home? : ant -> bool
; Check whether ant a is home
; (define (ant-at-home? a)
; ... (ant-weight a)
; ... (posn-at-home? (ant-loc a)) ...)
; (define (posn-at-home? p)
; ... (posn-x p) ... (posn-y p) ...)
(define (ant-at-home? a)
  (posn-at-home? (ant-loc a)))
(define (posn-at-home? p)
  (and (= (posn-x p) 0) (= (posn-y p) 0)))
(ant-at-home? (make-ant 0.001 (make-posn 0 0))) '= true
```

The shape of the template matches the shape of the data



Animals

(ant-at-home? (make-ant 0.001 (make-posn 1 1))) '= false

All animals need to eat...

• Define **feed-animal**, which takes an animal (snake, dillo, or ant) and feeds it (5 lbs, 2 lbs, or 0.001 lbs, respectively)

What is an **animal**?

Animal Data Definition

; An animal is either
; - snake
; - dillo
; - ant

The "either" above makes this a new kind of data definition:

data with varieties

Examples:

(make-snake 'slinky 10 'rats)

(make-dillo 2 true)

(make-ant 0.002 (make-posn 3 4))

Feeding Animals

```
; feed-animal : animal -> animal
                                                                 For the template step...
; To feed the animal a
                                                                                   (define (feed-animal a)
(define (feed-animal a)
                                                                                     ...)
  ...)
                                                                 • Is a compound data?
(feed-animal (make-snake 'slinky 10 'rats))
                                                                 • Technically yes, but the definition animal doesn't have
"should be" (make-snake 'slinky 15 'rats)
                                                                  make-something, so we don't use the compound-data template rule
(feed-animal (make-dillo 2 true))
"should be" (make-dillo 4 true)
(feed-animal (make-ant 0.002 (make-posn 3 4)))
"should be" (make-ant 0.003 (make-posn 3 4))
                   Template for Varieties
                                                                                    Questions for Varieties
Choice in the data definition
                                                                                   (define (feed-animal a)
                                                                                     (cond
                  ; An animal is either
                                                                                       [....]
                  ; - snake
```

```
; - dillo
```

; - ant

means cond in the template:

(define (feed-animal a) (cond [....] [....] [....]))

Three data choices means three cond cases

[....] [....]))

Template for Animals

How do we write a question for each case?

It turns out that

(define-struct snake (name weight food)) provides **snake**?

```
(snake? (make-snake 'slinky 5 'rats)) \rightarrow true
(snake? (make-dillo 2 true)) \rightarrow false
(snake? 17) \rightarrow false
```

Template

(define (feed-animal a)
 (cond
 [(snake? a) ...]
 [(dillo? a) ...]
 [(ant? a) ...]))

New template rule: varieties \Rightarrow cond

Now continue template case-by-case...

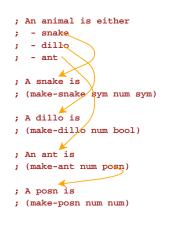
Template

```
(define (feed-animal a)
  (cond
    [(snake? a) ... (feed-snake a) ...]
    [(dillo? a) ... (feed-dillo a) ...]
    [(ant? a) ... (feed-ant a) ...]))
```

Remember: references in the data definition \Rightarrow template references

; An animal is either
; - snake
; - dillo
; - ant

Shapes of Data and Templates



```
(define (feed-animal a)
  (cond
   [(snake? a) ... (feed-snake a) ...]
   [(dillo? a) ... (feed-dillo a) ...]
   [(ant? a) ... (feed-ant a) ...]))
(define (feed-snake s)
  ... (snake-name s) ... (snake-weight s)
 ... (snake-food s) ...)
(define (feed-dillo d)
 ... (dillo-weight d)
 ... (dillo-alive? d) ...)
(define (feed-ant a)
 ... (ant-weight d)
 ... (feed-posn (ant-loc d)) ...)
(define (feed-posn p)
 \dots (posn-x p) \dots (posn-y p) \dots)
```

Design Recipe III

Data

• Understand the input data

Contract, Purpose, and Header

• Describe (but don't write) the function

Examples

• Show what will happen when the function is done

Template

• Set up the body based on the input data (and only the input)

Body

• The most creative step: implement the function body

Test

• Run the examples

Data

When the problem statement mentions ${\bf N}$ different varieties of a thing, write a data definition of the form

; A thing is
; - variety1
; ...

- 5
- ; varietyN

Examples

When the input data has varieties, be sure to pick each variety at least once.

```
; An animal is either
; - snake
; - dillo
; - ant
(feed-animal (make-snake 'slinky 10 'rats))
"should be" (make-snake 'slinky 15 'rats)
(feed-animal (make-dillo 2 true))
"should be" (make-dillo 4 true)
```

(feed-animal (make-ant 0.002 (make-posn 3 4)))
"should be" (make-ant 0.003 (make-posn 3 4))

Template

When the input data has varieties, start with cond

- N varieties \Rightarrow N cond lines
- Formulate a question to match each corresponding variety
- Continue template steps case-by-case

```
(define (feed-animal a)
  (cond
    [(snake? a) ...]
    [(dillo? a) ...]
    [(ant? a) ...]))
```

Template

When the input data has varieties, start with cond

- N varieties \Rightarrow N cond lines
- Formulate a question to match each corresponding variety
- Continue template steps case-by-case

When the data definition refers to a data definition, make the template refer to a template

```
(define (ant-at-home? a)
  ... (ant-weight a)
  ... (posn-at-home? (ant-loc a)) ...)
(define (posn-at-home? p)
  ... (posn-x p) ... (posn-y p) ...)
```

Template

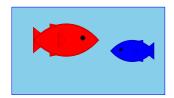
Aquarium

When the input data has varieties, start with cond

- N varieties \Rightarrow N cond lines
- Formulate a question to match each corresponding variety
- Continue template steps case-by-case

When the data definition refers to a data definition, make the template refer to a template

```
(define (feed-animal a)
  (cond
    [(snake? a) ... (feed-snake a) ...]
    [(dillo? a) ... (feed-dillo a) ...]
    [(ant? a) ... (feed-ant a) ...]))
```



For a fish, we only care about its weight, so for two fish:

Our zoo was so successful, let's start an aquarium

; An aquarium is
; (make-aq num num)
(define-struct aq (first second))

Aquarium Template

; An aquarium is ; (make-aq num num)

Generic template:

```
; func-for-aq : aquarium -> ...
; (define (func-for-aq a)
; ... (aq-first a) ... (aq-second a) ...)
```

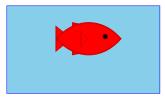
```
; aq-weight : aquarium -> num
(define (aq-weight a)
  (+ (aq-first a) (aq-second a)))
```

```
(aq-weight (make-aq 7 8)) "should be" 15
```

And so on, for many other simple aquarium functions...

Tragedy Strikes the Aquarium

Poor blue fish... now we have only one



Worse, we have to re-write all our functions...

; An aquarium is
; (make-aq num)
(define-struct aq (first))

Aquarium Template, Revised

; An aquarium is

The Aquarium Expands

Hooray, we have two new fish!

```
; (make-aq num)
; func-for-aq : aquarium -> ...
; (define (func-for-aq a)
; ... (aq-first a) ...)
; aq-weight : aquarium -> num
(define (aq-weight a)
      (aq-first a))
```

```
(aq-weight (make-aq 7)) "should be" 7
```

And so on, for **all** of the aquarium functions...

Unfortunately, we have to re-re-write all our functions...

; An aquarium is ; (make-aq num num num) (define-struct aq (first second third))

A Flexible Aquarium Representation

Structs as Boxes

Pictorially,

- **define-struct** lets us define a new kind of box
- The box can have as many compartments as we want, but we have to pick how many, once and for all

(define-struct snake (name weight food))



(define-struct ant (weight loc))



Our data choice isn't working

- An aquarium isn't just 1 fish, 2 fish, or 100 fish it's a collection containing an arbitrary number of fish
- No data definition with just 1, 2, or 100 numbers will work

To represent an aquarium, we need a *list* of numbers

We don't need anything new in the language, just a new idea

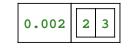
Boxes Stretch

Packing Boxes

The boxes stretch to fit any one thing in each slot:

'slinky 12 'rats

Even other boxes:

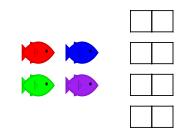


Still, the number of slots is fixed

Suppose that

- You have four things to pack as one
- You only have 2-slot boxes
- Every slot must contain exactly one thing

How can you create a single package?



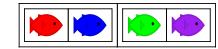
Packing Boxes

This isn't good enough



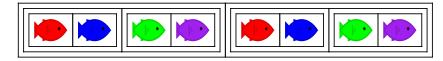
because it's still two boxes...

But this works!

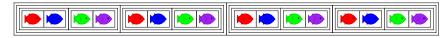


Packing Boxes

And here's 8 fish:



And here's 16 fish!



But what if we just add 1 fish, instead of doubling the fish?

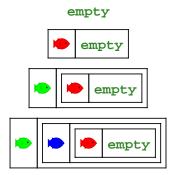
But what if we have 0 fish?

General Strategy for Packing Boxes

Here's a general strategy:

- For 0 fish, use empty
- If you have a package and a new fish, put them together

To combine many fish, start with empty and add fish one at a time



General Strategy for a List of Numbers

To represent the aquarium as a list of numbers, use the same idea:

- For 0 fish, use empty
- If you have a list and a number, put them together with make-bigger-list

empty

(make-bigger-list 10 empty)

(make-bigger-list 5 (make-bigger-list 10 empty))

(make-bigger-list 7 (make-bigger-list 5 (make-bigger-list 10 empty)))

List of Numbers

- ; A list-of-num is either
- ; empty
- ; (make-bigger-list num list-of-num)
- (define-struct bigger-list (first rest))

List of Numbers

; A list-of-num is either
; - empty
; - (make-bigger-list num list-of-num)
(define-struct bigger-list (first rest))

Generic template:
; func-for-lon : list-of-num -> ...
(define (func-for-lon 1)
 ...)

List of Numbers

```
; A list-of-num is either
; - empty
; - (make-bigger-list num list-of-num)
(define-struct bigger-list (first rest))
```

Generic template:

```
; func-for-lon : list-of-num -> ...
(define (func-for-lon 1)
  (cond
     [(empty? 1) ...]
     [(bigger-list? 1) ...]))
```

List of Numbers

```
; A list-of-num is either
; - empty
; - (make-bigger-list num list-of-num)
(define-struct bigger-list (first rest))
```

```
Generic template:
```

```
; func-for-lon : list-of-num -> ...
(define (func-for-lon 1)
  (cond
    [(empty? 1) ...]
    [(bigger-list? 1)
    ... (bigger-list-first 1)
    ... (bigger-list-rest 1)
    ...]))
```

List of Numbers

```
; A list-of-num is either
; - empty
; - (make-bigger-list num list-of-num)
(define-struct bigger-list (first rest))
```

```
Generic template:
```

```
; func-for-lon : list-of-num -> ...
(define (func-for-lon 1)
  (cond
    [(empty? 1) ...]
    [(bigger-list? 1)
    ... (bigger-list-first 1)
    ... (bigger-list-rest 1)
    ...]))
```

List of Numbers

```
; A list-of-num is either
; - empty
; - (make-bigger-list num list-of-num)
(define-struct bigger-list (first rest))
```

```
Generic template:
```

```
; func-for-lon : list-of-num -> ...
(define (func-for-lon 1)
  (cond
    [(empty? 1) ...]
    [(bigger-list? 1)
    ... (bigger-list-first 1)
    ... (func-for-lon (bigger-list-rest 1))
    ...]))
```

```
Aquarium Weight
                                                                            Aquarium Weight
; aq-weight : list-of-num -> num
                                                              ; aq-weight : list-of-num -> num
; Sums the fish weights in 1
                                                              ; Sums the fish weights in 1
                                                              (define (aq-weight 1)
(define (aq-weight 1)
  ...)
                                                                ...)
                                                              (aq-weight empty) "should be" 0
              Aquarium Weight
                                                                            Aquarium Weight
; ag-weight : list-of-num -> num
                                                              ; ag-weight : list-of-num -> num
; Sums the fish weights in 1
                                                              ; Sums the fish weights in 1
                                                              (define (aq-weight 1)
(define (aq-weight 1)
                                                                ...)
  ...)
(aq-weight empty) "should be" 0
                                                              (aq-weight empty) "should be" 0
(aq-weight (make-bigger-list 2 empty))
                                                              (aq-weight (make-bigger-list 2 empty))
"should be" 2
                                                              "should be" 2
                                                              (aq-weight (make-bigger-list 5 (make-bigger-list 2 empty)))
                                                              "should be" 7
```

Aquarium Weight

```
; aq-weight : list-of-num -> num
; Sums the fish weights in l
(define (aq-weight l)
  (cond
    [(empty? l) ...]
    [(bigger-list? l)
    ... (bigger-list-first l)
    ... (aq-weight (bigger-list-rest l))
    ...]))
```

```
(aq-weight empty) "should be" 0
```

```
(aq-weight (make-bigger-list 2 empty))
"should be" 2
```

```
(aq-weight (make-bigger-list 5 (make-bigger-list 2 empty)))
"should be" 7
```

Aquarium Weight

```
; aq-weight : list-of-num -> num
; Sums the fish weights in l
(define (aq-weight 1)
  (cond
   [(empty? 1) 0]
   [(bigger-list? 1)
    (+ (bigger-list-first 1)
        (aq-weight (bigger-list-rest 1)))]))
Try examples in the stepper
(aq-weight empty) "should be" 0
(aq-weight (make-bigger-list 2 empty))
```

```
"should be" 2
```

```
(aq-weight (make-bigger-list 5 (make-bigger-list 2 empty)))
"should be" 7
```

Aquarium Weight

```
; aq-weight : list-of-num -> num
; Sums the fish weights in l
(define (aq-weight l)
  (cond
  [(empty? l) 0]
  [(bigger-list? l)
    (+ (bigger-list-first l)
        (aq-weight (bigger-list-rest l)))]))
```

(aq-weight empty) "should be" 0

(aq-weight (make-bigger-list 2 empty))
"should be" 2

(aq-weight (make-bigger-list 5 (make-bigger-list 2 empty)))
"should be" 7

Pipes

• Pipes end in faucets (open or closed) and sometimes branch



Pipes

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Pipes

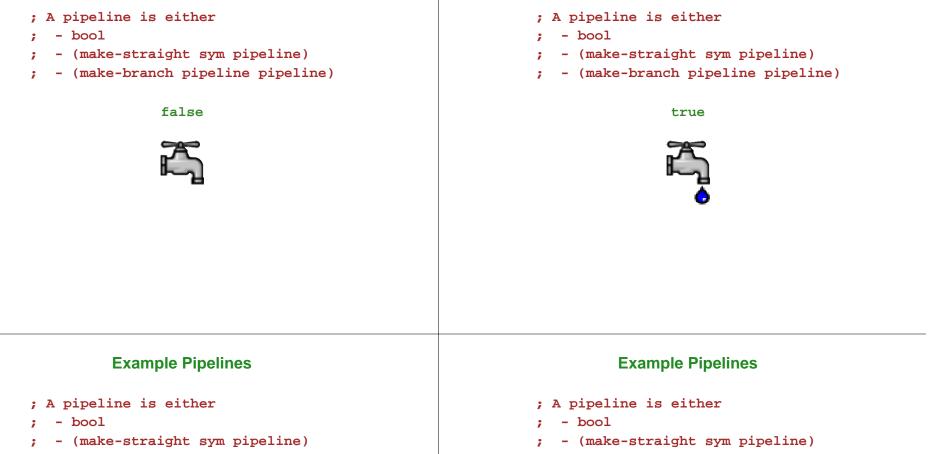
• Pipes end in faucets (open or closed) and sometimes branch



- ; A pipeline is either
- ; bool
- (make-straight sym pipeline)
- ; (make-branch pipeline pipeline)
- (define-struct straight (kind next))
- (define-struct branch (next1 next2))

Example Pipelines

Example Pipelines



; - (make-branch pipeline pipeline)

(make-straight 'copper false)



; - (make-branch pipeline pipeline)

(make-straight 'copper

(make-straight 'lead false))



Example Pipelines

- ; A pipeline is either
- ; bool
- ; (make-straight sym pipeline)
- ; (make-branch pipeline pipeline)

(make-branch

```
(make-branch (make-straight 'copper true)
    false)
(make-branch false
    false))
```



; A pipeline is either ; - bool ; - (make-straight sym pipeline) ; - (make-branch pipeline pipeline) (define (func-for-pipeline pl) (cond [(boolean? pl) ...] [(straight? pl) ... (straight-kind pl) ... (func-for-pipeline (straight-next pl)) ...] [(branch? pl) ... (func-for-pipeline (branch-next1 pl)) ... (func-for-pipeline (branch-next2 pl)) ...]))

Programming with Pipelines

Pipeline Examples

- Implement the function **water-running?** which takes a pipeline and determines whether any faucets are open
- Implement the function **modernize** which takes a pipeline and converts all **'lead** straight pipes to **'copper**
- Implement the function **off** which takes a pipeline and turns off all the faucets
- Implement the function **lead-off** which takes a pipeline and turns off all the faucets that receive water through a lead pipe
- Implement the function twice-as-long which takes a pipeline and inserts a 'copper straight pipe before every existing piece of the pipeline