

Page-Replacement Algorithms

A ***page replacement algorithm*** picks a page to paged out and free up a frame

- **FIFO** — first-in, first-out
- **Optimal** — the one that leads to the least faults
- **LRU** — least-recently used
- **LRU** approximations

FIFO

7	0	1	2	0	3	0	4	2	3	0	3	2	1	2	0	1	7	0	1
7	0	1	2	2	3	0	4	2	3	0	0	0	1	2	2	2	7	0	1
	7	0	1	1	2	3	0	4	2	3	3	3	0	1	1	1	2	7	0
		7	0	0	1	2	3	0	4	2	2	2	3	0	0	0	1	2	7

1	2	3	4	1	2	5	1	2	3	4	5
1	2	3	4	1	2	5	5	5	3	4	4
	1	2	3	4	1	2	2	2	5	3	3
		1	2	3	4	1	1	1	2	5	5

1	2	3	4	1	2	5	1	2	3	4	5
1	2	3	4	4	4	5	1	2	3	4	5
	1	2	3	3	3	4	5	1	2	3	4
		1	2	2	2	3	4	5	1	2	3
			1	1	1	2	3	4	5	1	2

Belady's anomaly:
 more frames
 can be worse

Optimal

7	0	1	2	0	3	0	4	2	3	0	3	2	1	2	0	1	7	0	1
7	7	7	2	2	2	2	2	2	2	2	2	2	2	2	2	2	7	7	7
	0	0	0	0	0	0	4	4	4	0	0	0	0	0	0	0	0	0	0
		1	1	1	3	3	3	3	3	3	3	3	1	1	1	1	1	1	1

1	2	3	4	1	2	5	1	2	3	4	5
1	1	1	1	1	1	1	1	1	1	1	1
	2	2	2	2	2	2	2	2	3	4	4
		3	4	4	4	5	5	5	5	5	5

1	2	3	4	1	2	5	1	2	3	4	5
1	1	1	1	1	1	1	1	1	1	1	1
	2	2	2	2	2	2	2	2	2	2	2
		3	3	3	3	3	3	3	3	4	4
			4	4	4	5	5	5	5	5	5

But how do you predict the future?

LRU

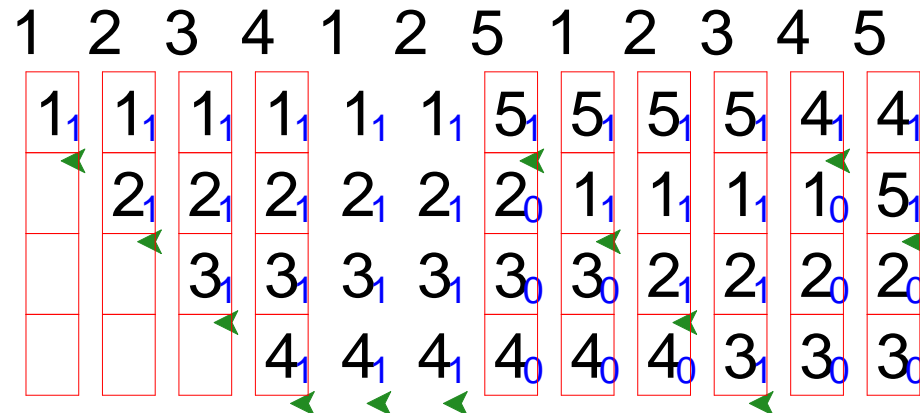
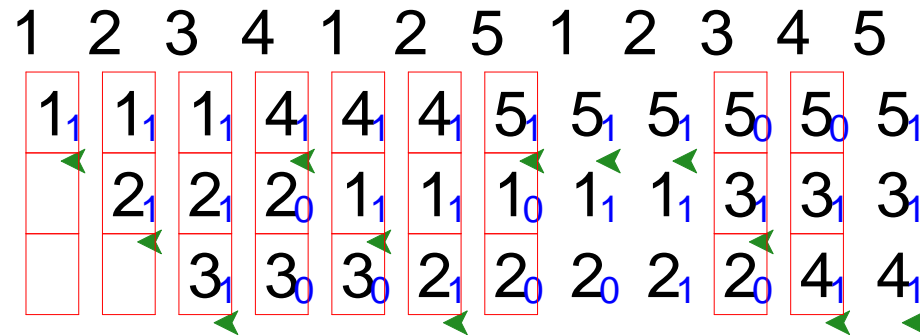
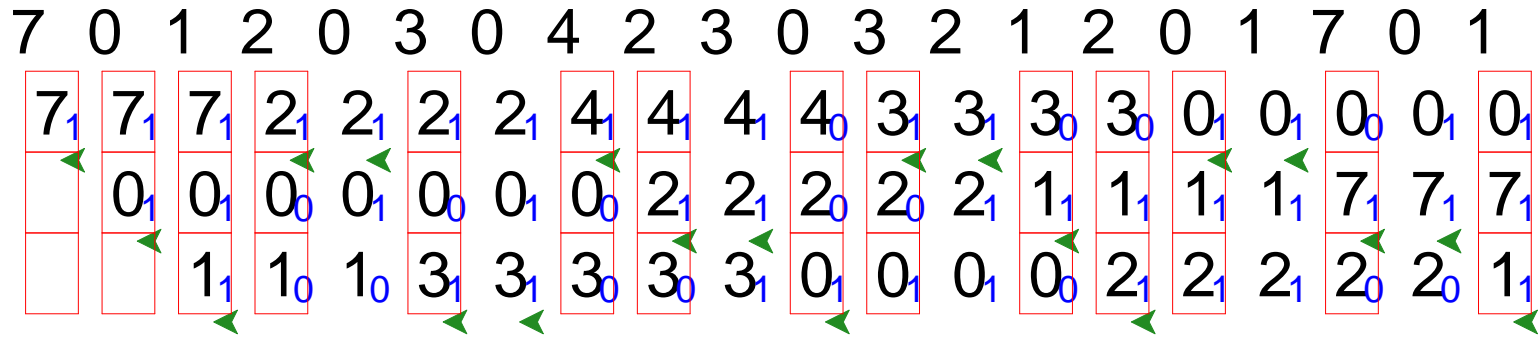
7	0	1	2	0	3	0	4	2	3	0	3	2	1	2	0	1	7	0	1
7 ₀	7 ₁	7 ₂	2 ₀	2 ₁	2 ₂	2 ₃	4 ₀	4 ₁	4 ₂	0 ₀	0 ₁	0 ₂	1 ₀	1 ₁	1 ₂	1 ₀	1 ₁	1 ₂	1 ₀
	0 ₀	0 ₁	0 ₂	0 ₀	0 ₁	0 ₀	0 ₁	0 ₂	3 ₀	3 ₁	3 ₀	3 ₁	3 ₂	3 ₃	0 ₀	0 ₁	0 ₂	0 ₀	0 ₁
		1 ₀	1 ₁	1 ₂	3 ₀	3 ₁	3 ₂	2 ₀	2 ₁	2 ₂	2 ₃	2 ₀	2 ₁	2 ₀	2 ₁	2 ₂	7 ₀	7 ₁	7 ₂

1	2	3	4	1	2	5	1	2	3	4	5
1 ₀	1 ₁	1 ₂	4 ₀	4 ₁	4 ₂	5 ₀	5 ₁	5 ₂	3 ₀	3 ₁	3 ₂
	2 ₀	2 ₁	2 ₂	1 ₀	1 ₁	1 ₂	1 ₀	1 ₁	1 ₂	4 ₀	4 ₁
		3 ₀	3 ₁	3 ₂	2 ₀	2 ₁	2 ₂	2 ₀	2 ₁	2 ₂	5 ₀

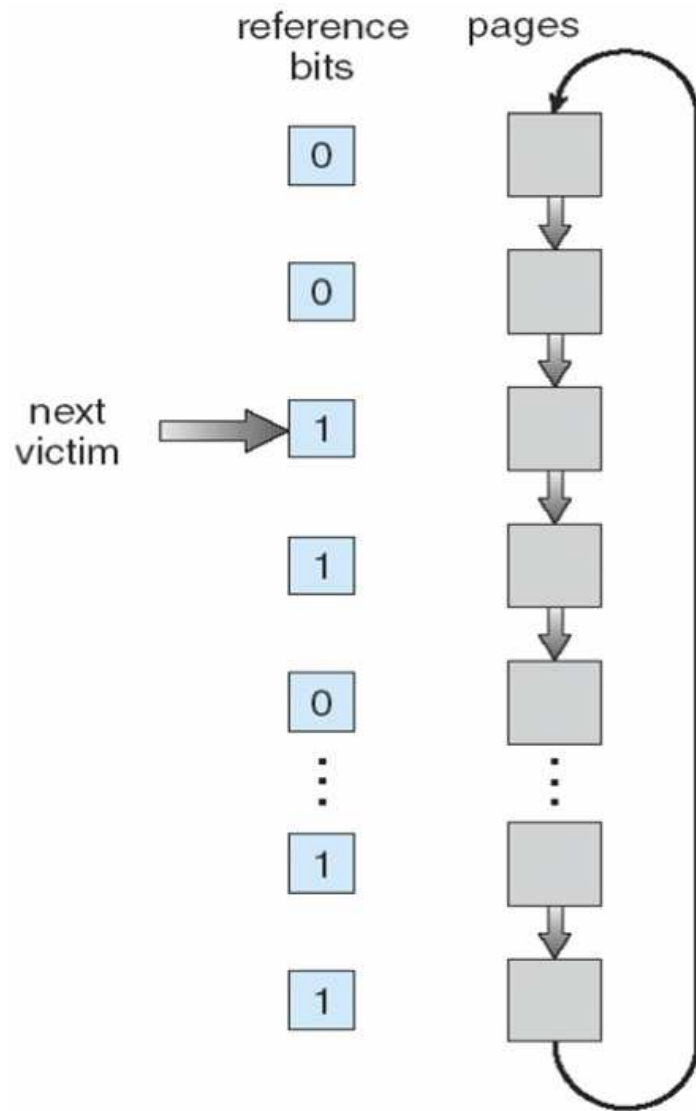
1	2	3	4	1	2	5	1	2	3	4	5
1 ₀	1 ₁	1 ₂	1 ₃	1 ₀	1 ₁	1 ₂	1 ₀	1 ₁	1 ₂	1 ₃	5 ₀
	2 ₀	2 ₁	2 ₂	2 ₃	2 ₀	2 ₁	2 ₂	2 ₀	2 ₁	2 ₂	2 ₃
		3 ₀	3 ₁	3 ₂	3 ₃	5 ₀	5 ₁	5 ₂	5 ₃	4 ₀	4 ₁
			4 ₀	4 ₁	4 ₂	4 ₃	4 ₄	4 ₅	3 ₀	3 ₁	3 ₂

Searching all times is expensive on fault; keeping a sorted list is expensive on access

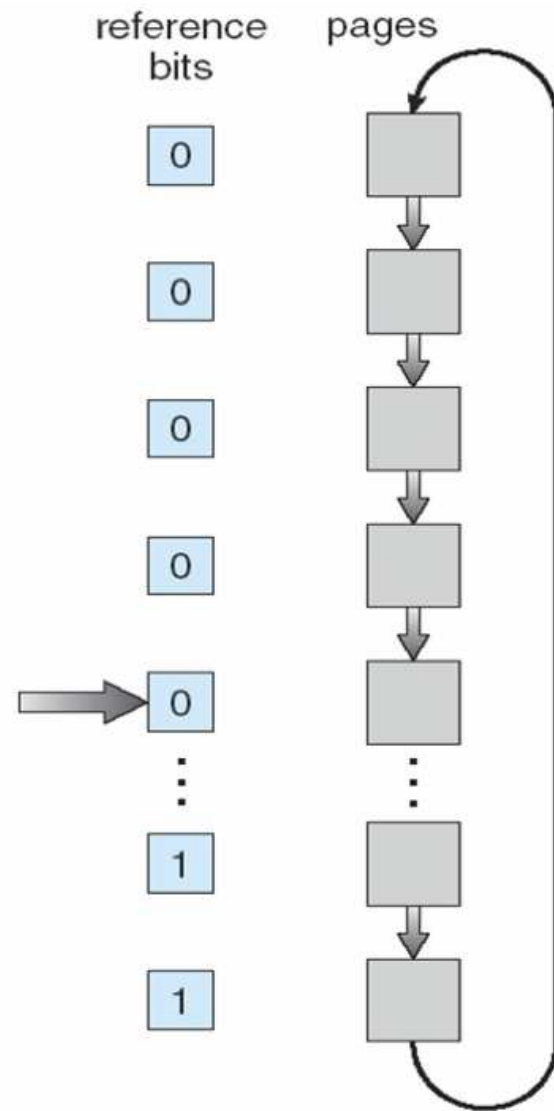
Second Chance



Second Chance



(a)



(b)

Enhanced Second Chance

Track both use and modifies (relative to copy on disk):

- Not used, Not modified — good to replace
- Not used, Modified — ok, but have to write out
- Used, Not modified — rather keep it
- Used, Modified — really rather keep it

Allocating Frames

Frame allocation can be defined orthogonal to page replacement:

- Allocation algorithm determines candidate pages to evict
- Replacement algorithm picks a specific page to evict
- **Local allocation:** each process has some frames
- **Global allocation:** frames shared among all processes

Thrashing

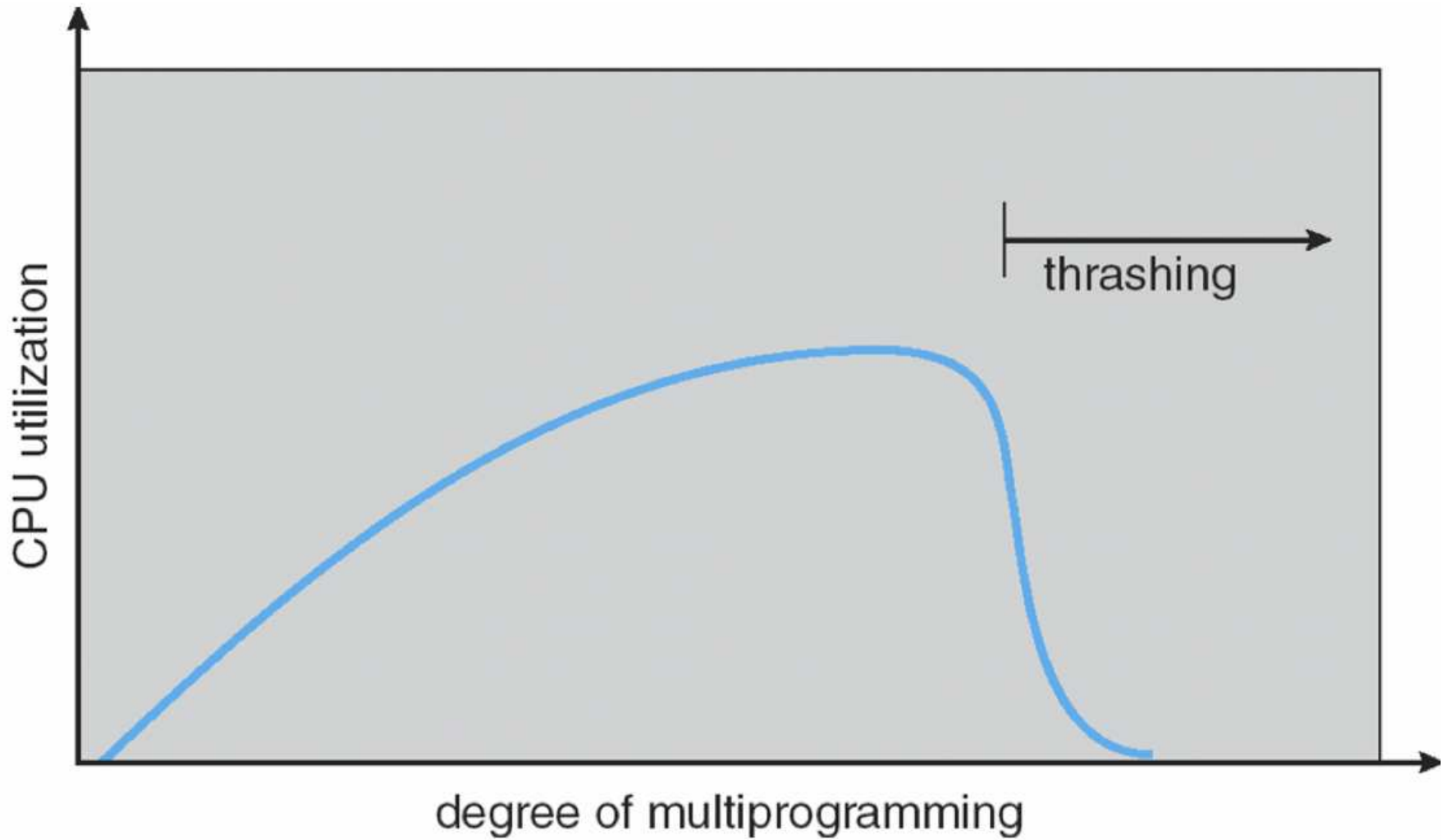
```
#define SIZE (1024*1024*32)

int main (void)
{
    while (1) {
        char *x;
        int i;

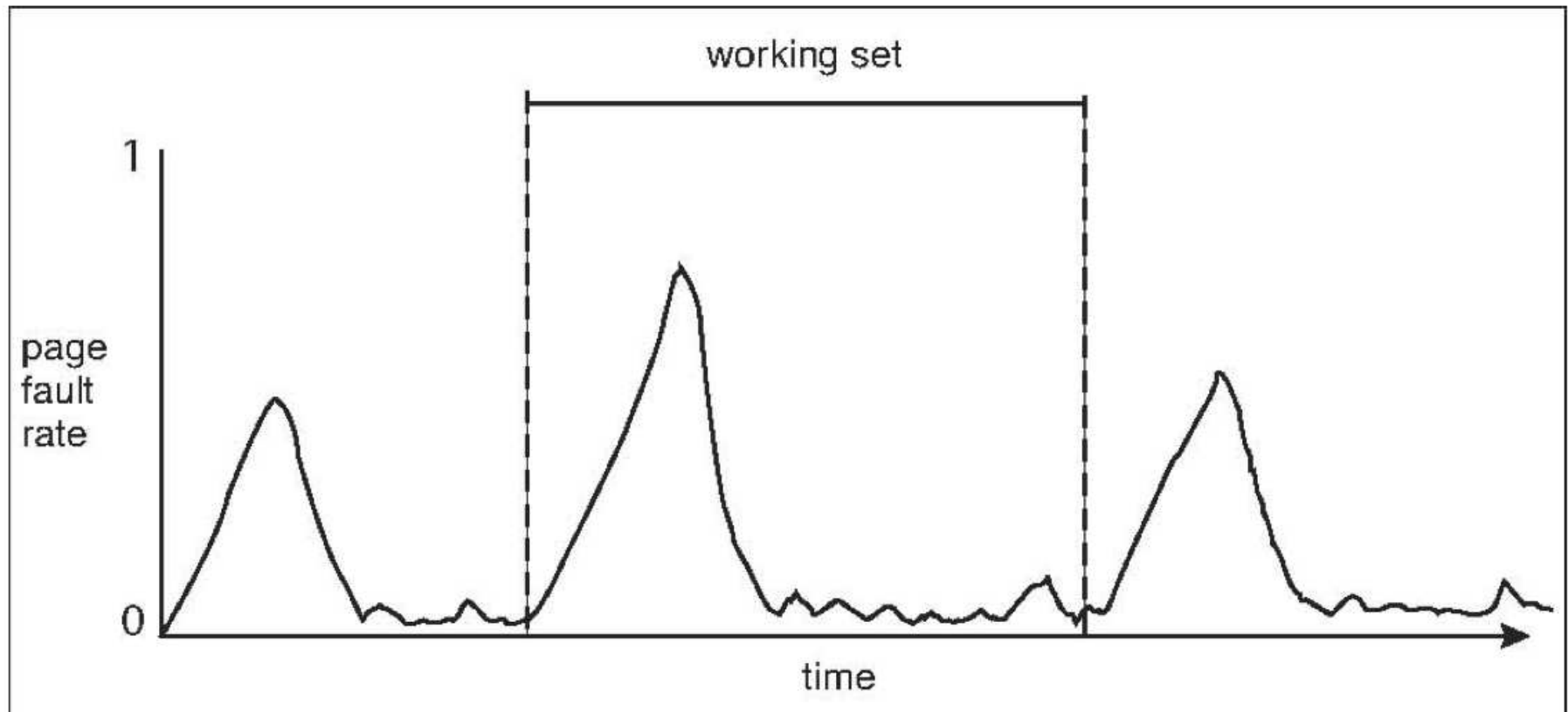
        x = (char *) malloc (SIZE);
        for (i=0; i<SIZE; i++) x[i] = 1;

        fork();
    }
}
```

Thrashing



Measuring Working Set



Interaction with I/O

- Some memory is used for a disk cache
- Communicating with an I/O device may require physical memory \Rightarrow lock bits
- Memory-mapped files \Rightarrow shared memory