# Mid-Term Exam 2 

CS 3520, Fall 2000 Edited for Fall 2001

Name: $\qquad$

Instructions: You have one hour and twenty minutes to complete this open-book, open-note, closedcomputer exam. Please write all answers in the provided space, plus the back of the exam if necessary.

1) Given the following expression in the language we have been implementing:
```
letrec \(g=\operatorname{proc}(y)(g-(y, 1))\)
    in let \(x=f\)
        \(\mathrm{f}=\mathrm{g}\)
        in let \(f=\operatorname{proc}(z)(f+(x, z))\)
            in (g (f m) )
```

a) Draw arrows on the above expression from each bound variable to its binding occurrence.
b) List the free variables: and bound variables:
c) Re-write the above expression, replacing each bound variable with its lexical address. A lexical address is of the form $@(d, o)$ where $d$ is the lexical depth and $o$ is the offset at that depth.
2) Given the following expression for the call-by-value variant of our language:

```
let g = proc(z)z
    x = 10
in let f = proc(w)(g w)
    in (f x)
```

a) Describe the closure bound to $f$ at the point where ( $f x$ ) is the current expression.

* Argument variables:
* Body expression:
* Environment:
b) Describe the environment at the point during evaluation where ( g w ) is the current expression.

3) Given the following expression:
```
let f = let y = 7
    in proc(x)+(x,y)
    in (f 3)
```

Describe a trace of the evalaution in terms of arguments to an eval-expression interpreter function for every call. For literal, variable, and proc expressions, show the result.

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4) Given the following expression:

```
let x = 0
    in let f = proc(y)+(y,y)
            in (f { set x = +(x,7) ; x } )
```

a) What is the value of the expression in a call-by-value language?
b) What is the value of the expression in a call-by-name language?
c) What is the value of the expression in a call-by-need language?
5) Find and justify a type for the following expression:

$$
\text { ((proc(int y)proc(bool b)if b then } 0 \text { else y 8) false) }
$$

6) In the typed expression

$$
\operatorname{proc}\left(T_{1} \mathrm{a}, T_{2} \mathrm{~b}\right) \text { if a then } \operatorname{proc}(\text { int } \mathrm{y}) \mathrm{y} \text { else } \mathrm{b}
$$

what types must replace $T_{1}$ and $T_{2}$ so that the expression has a type?

$$
T_{1}=
$$

$$
T_{2}=
$$

