

Analyzing Scalability of Parallel Algorithm and Architectures

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Objectives of this paper

- 1.Survey various metrics
- 2.Relations between these metrics
- 3.Critically asses these metrics
- 4.Directions for future research

Typical metrics

- Amdahl's law
- Isoefficiency function
- Gustafson
- Zorbas
- Isospeed
- Sizeup

Definition

- W is problem size
- $T_p(W,p)$ is Parallel execution time on p processors for W problem size
- $T_s(W)$ is Serial execution time for W problem size
- $T_0(W,p)$ is Overhead
- $T_0 = pT_p - T_s$
- Efficiency $E = T_s/pT_p = 1/(1+T_0/TS);$

• Amdahl's law

- If s is serial fraction in an algorithm.
Then the maximum speedup is bounded by $1/s$.

Isoefficiency

- Solve fixed size problem.

Efficiency decrease when processor increase.

- If the problem size increase on fixed number of processors, then the efficiency increase.

- If the system is 'scalable parallel system'

Efficiency E can be maintained at some fixed value for increasing of number of processors and problem size

Isoefficiency

- $f_E(p)$ is Isoefficiency function
- $f_E(p)$ return problem size that can maintain efficiency E on number of p processors.
- If $f_E(p)$ grows exponential, then it's poorly scalable
- If $f_E(p)$ grows linearly, then it's highly scalable

•Gustafson

- Scaled speedup
- Speedup obtained when the problem size is increased linearly with the number of processors.
- If speedup curve is good(close to linear)
then the system is scalable system.

•Gustafson

- Two ways to increase problem size
 1. the size of memory be used.
 - 2.the size of problem growths with p subject to an upper bound on execution time.

• Zorbas

- This metric consider the system is ideally scalable if system's overhead function remains constant when the problem size is increased sufficiently fast with respect to number of processors

Isospeed

- Isospeed measure trying to find problem size W' , for the average unit speed of computation remain constant when number of processors increased to p' from p
- $\text{isospeed}(p, p') = p'W/pW'$
- For perfectly parallelizable algorithm with no communication $\text{isospeed}(p, p') = 1$
- $W' = p'W/p$

Sizeup

- Unfair measure
- Sizeup is ratio of

Size of problem solved on the parallel computer

Size of problem solved on the sequential computer
in fixed time

- Is there exists one measure that is better than all others?
- NO

Examples

- If problem size fixed, and one is trying to solve by increase number of processors, in this case, try to find optimal number of processors, Amdahl's law is good measure
- If number of processor is fixed, then use isoefficiency function to find best problem size is good measure

Hardware Factor

- Improve technology in only one direction may not be a wise idea
- Increasing speed of the processors alone without improving the communication speed will result in diminishing returns in terms of overall speedup and efficiency.

Thoughts

- How to define problem size
- How to increase problem size

Ideas

- Gustafson's suggestion:
 1. memory
 2. execution time on sequential computer
- Others:
 1. If there are iterations, increase iteration.

Conclusion

- No single scalability metric would be better than all others
- Different measures will be useful in different contexts and further research is needed along several directions
- Hardware cost factors in the scalability analysis is important but still very preliminary