

Asmt 5: Frequent Items

Turn in through Canvas by 2:45pm:

Wednesday, Feb 26

100 points

Overview

In this assignment you will explore finding frequent items in data sets, with emphasis on streaming techniques designed to work at enormous scale. For simplicity you will work on more manageably sized data sets, and simulate the stream by just processing with a for loop.

You will use two data sets for this assignment:

- <http://www.cs.utah.edu/~jeffp/teaching/cs5140/A5/S1.txt>
- <http://www.cs.utah.edu/~jeffp/teaching/cs5140/A5/S2.txt>

The first data set S1 has a set of $m = 3,000,000$ characters, and the second one S2 has $m = 4,000,000$ characters. The order of the file represents the order of the stream.

As usual, it is highly recommended that you use LaTeX for this assignment. If you do not, you may lose points if your assignment is difficult to read or hard to follow. Find a sample form in this directory: <http://www.cs.utah.edu/~jeffp/teaching/latex/>

1 Streaming Algorithms

A (40 points): Run the Misra-Gries Algorithm (see **L11.3.1**) with $(k - 1) = 9$ counters on streams S1 and S2. Report the output of the counters at the end of the stream. In addition to each counter report the estimated ratio of each label using the estimated count/ m .

In each stream, use just the counters to report which characters *might* occur at least 20% of the time, and which must occur at least 20% of the time.

B (40 points): Build a Count-Min Sketch (see **L12.1.1**) with $k = 10$ counters using $t = 5$ hash functions. Run it on streams S1 and S2.

For both streams, report the estimated counts for characters **a**, **b**, and **c**. In addition to each counter report the estimated ratio of each of these labels using the estimated count/ m . Just from the output of the sketch, with probably $1 - \delta = 31/32$ (that is assuming the randomness in the algorithm does not do something bad), which objects *might* occur at least 20% of the time, and which objects *must* occur at least 20% of the time.

C (10 points): How would your implementation of these algorithms need to change (to answer the same questions) if each object of the stream was a “word” seen on Twitter, and the stream contained all tweets concatenated together?

D (10 points): Describe one advantage of the Count-Min Sketch over the Misra-Gries Algorithm.

2 BONUS

The exact heavy-hitter problem is as follows: return *all* objects that occur more than 10% of the time. It cannot return any false positives or any false negatives. In the streaming setting, this requires $\Omega(\min\{m, n\})$ space if there are n objects that can occur and the stream is of length m .

A: (1 point) A 2-Pass streaming algorithm is one that is able to read all of the data in-order exactly twice, but still only has limited memory. Describe a small space algorithm to solve the exact heavy hitter problem, i.e., with $\epsilon = 0$, (say for $\phi = 10\%$ threshold).

B: (2 points) Provide an upper bound for the probability that at least one student gets a really bad estimate for the CountMin Sketch where the count estimate for **a**, **b**, and **c** are all the same since they always collide. As in the question 1B use $k = 10$ and $t = 5$, and assume perfect hash functions. And take into account that there are $n = 125$ students in the class, and this is a problem if it happens to any one of them.