Suppose that a patient can have a symptom $S$ that can be caused by two different diseases $A$ and $B$. Disease $A$ is much rarer, but there is a test $T$ that tests for the presence of $A$. The Bayes' Net and corresponding conditional probability tables are shown below.


| $A$ | $P(A)$ |
| :---: | :---: |
| $+a$ | 0.1 |
| $-a$ | 0.9 |
| $B$ | $P(B)$ |
| $+b$ | 0.5 |
| $-b$ | 0.5 |


| $A$ | $T$ | $P(T \mid A)$ |
| :---: | :---: | :--- |
| $+a$ | $+t$ | 1 |
| $+a$ | $-t$ | 0 |
| $-a$ | $+t$ | 0.2 |
| $-a$ | $-t$ | 0.8 |


| $A$ | $B$ | $S$ | $P(S \mid A, B)$ |
| :---: | :---: | :---: | :--- |
| $+a$ | $+b$ | $+s$ | 1 |
| $+a$ | $+b$ | $-s$ | 0 |
| $+a$ | $-b$ | $+s$ | 0.8 |
| $+a$ | $-b$ | $-s$ | 0.2 |
| $-a$ | $+b$ | $+s$ | 1 |
| $-a$ | $+b$ | $-s$ | 0 |
| $-a$ | $-b$ | $+s$ | 0 |
| $-a$ | $-b$ | $-s$ | 1 |

1. From the Baye's Net structure, what is $P(A, T, B, S)$ ?
2. What is $P(-a,-t,+b,+s)$ ?
3. What is the probability that a patient has disease $+a$ given that they have disease $+b$ ?
4. What is the probability that a patient has disease $+a$ given that they have symptoms $+s$, disease $+b$, and test $+t$ returns positive?
5. What is the probability that a patient has disease $+a$ given that they have symptom $+s$ and test $+t$ returns positive?
