

# COMPLETE MONITORS FOR GRADUAL TYPES

✦ Ben Greenman  
🌐 at **Northeastern**

Matthias Felleisen  
🌐 at **Northeastern**

Christos Dimoulas  
🌐 at **Northwestern**

# COMPLETE MONITORS FOR GRADUAL TYPES

a careful analysis  
of the mixed-typed  
design space

✦ Ben Greenman  
at **Northeastern**

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Type soundness is not enough

Complete monitoring\* is crucial  
for **meaningful** gradual types

"Incomplete" monitoring provides a way to  
**measure** the quality of blame errors

\*from ESOP 2012

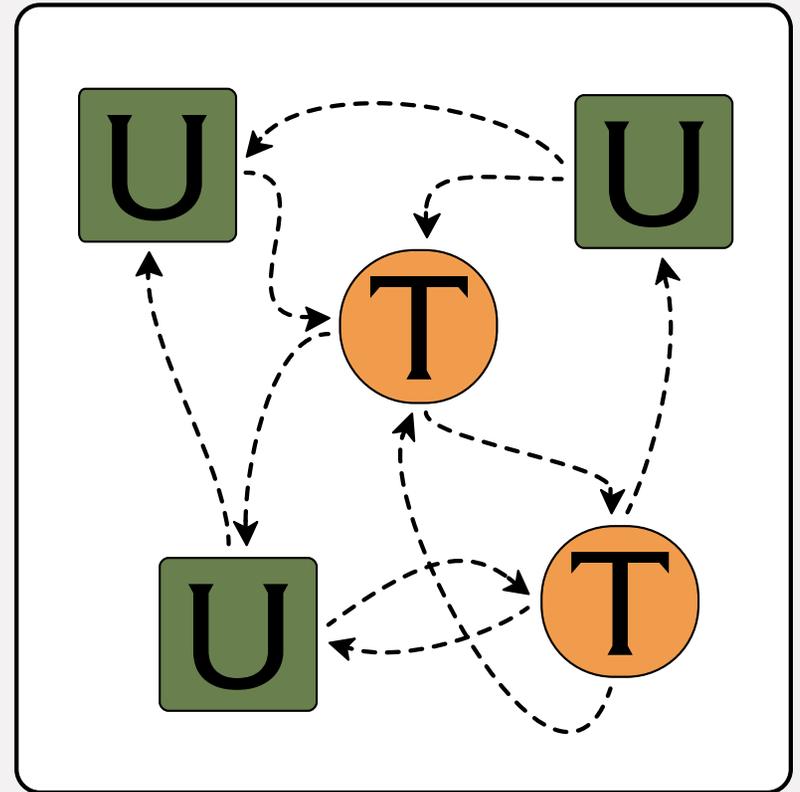
# Mixed-Typed Language

# Mixed-Typed Language

**U** = untyped code

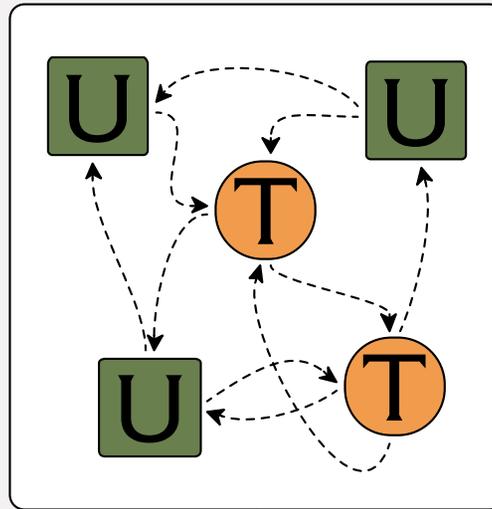
**T** = simply-typed code

(no 'Dynamic' type)



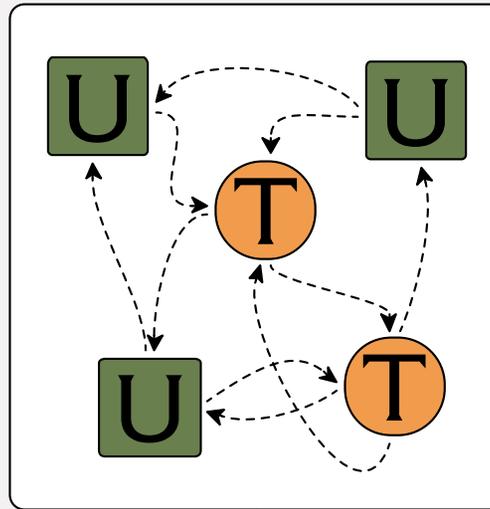
Untyped/Typed mix

# A Few Motivations



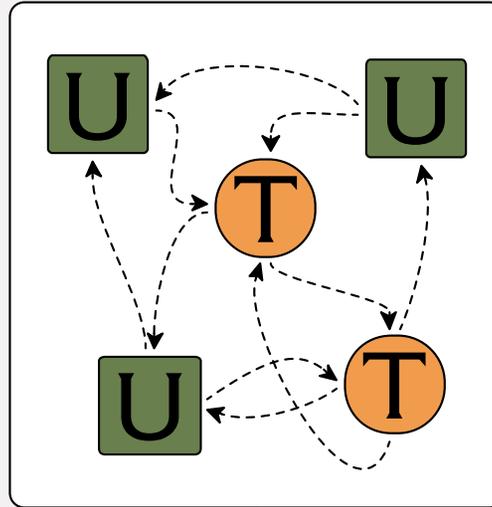
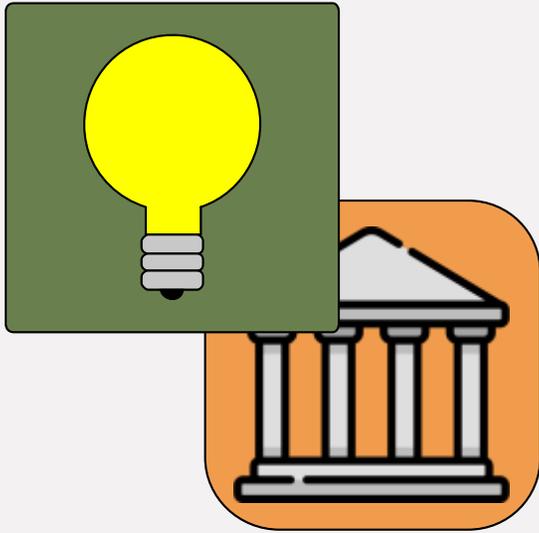
# A Few Motivations

Prototyping



# A Few Motivations

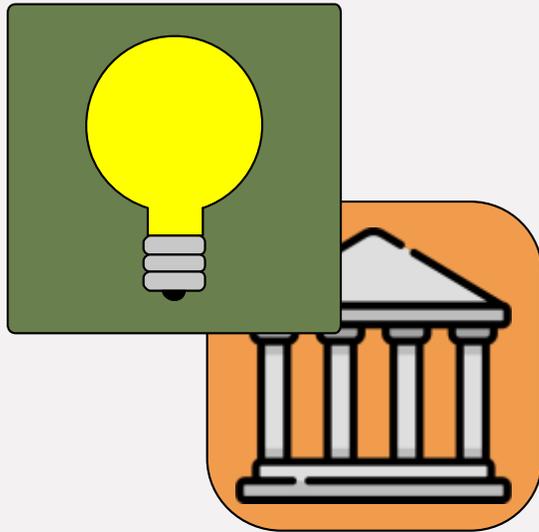
Prototyping



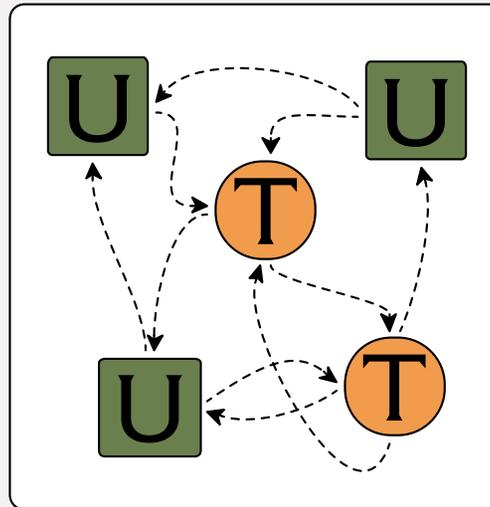
write untyped code,  
rely on types

# A Few Motivations

Prototyping



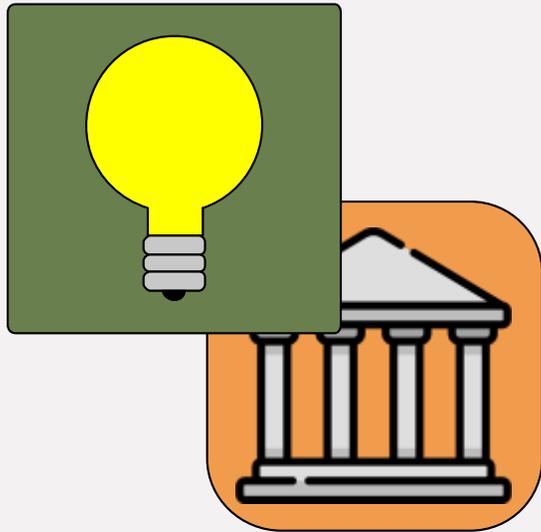
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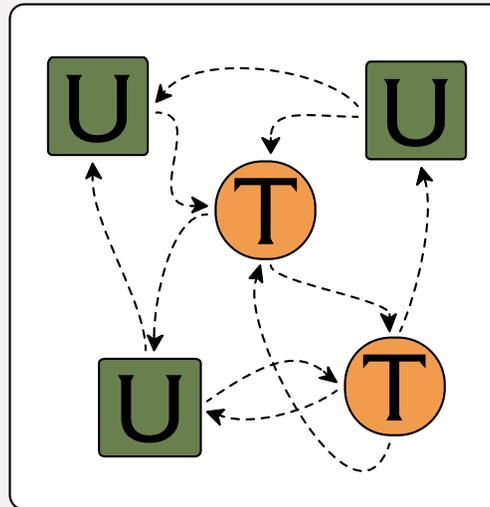
Re-Use

# A Few Motivations

Prototyping



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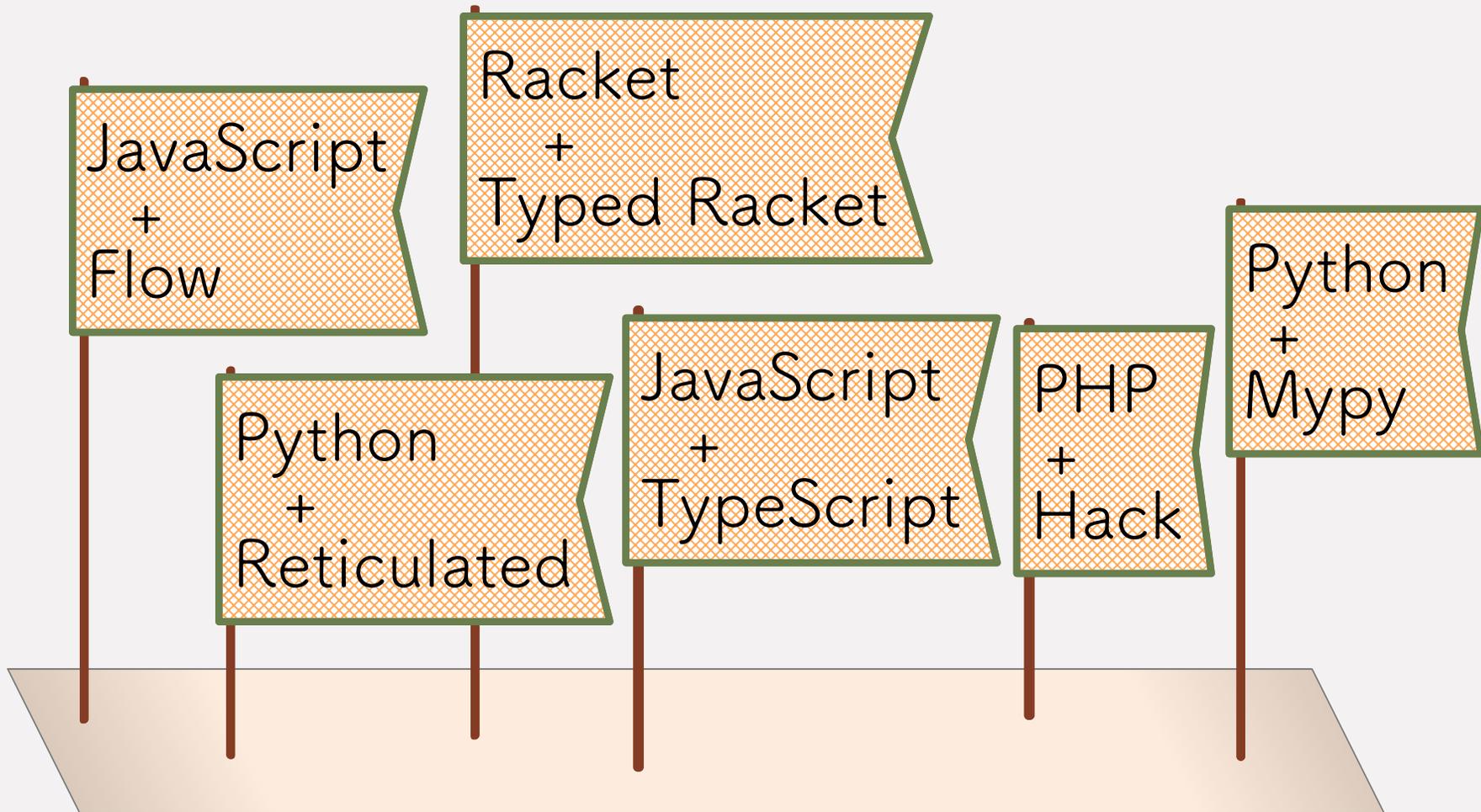


Re-Use

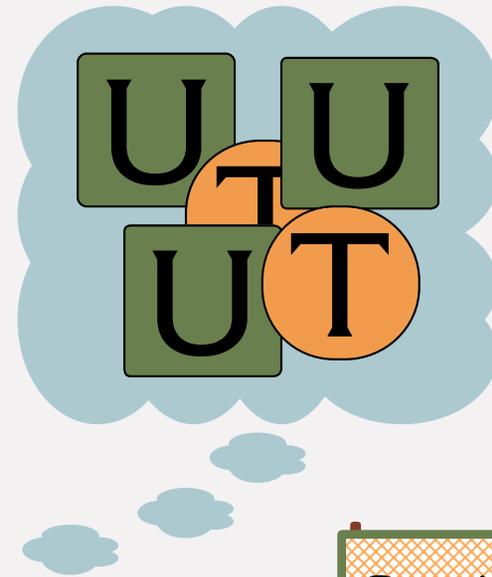


write typed code,  
use old libraries

# Many Implementations ...



Many Implementations ...  
... difficult to compare



JavaScript  
+  
Flow

Racket  
+  
Typed Racket

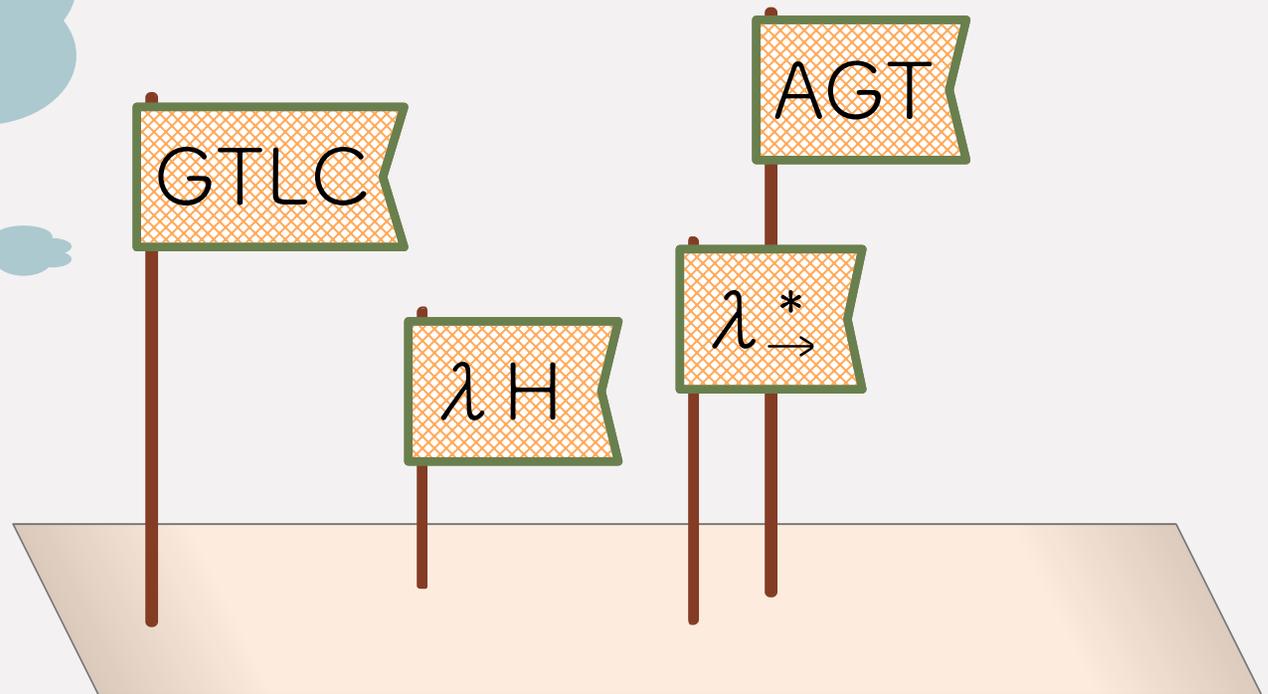
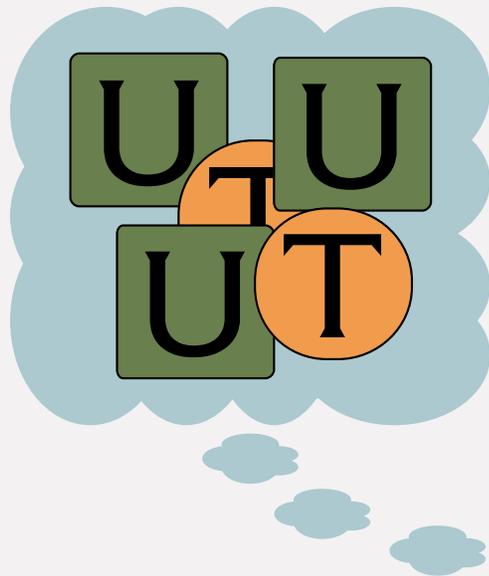
Python  
+  
Reticulated

JavaScript  
+  
TypeScript

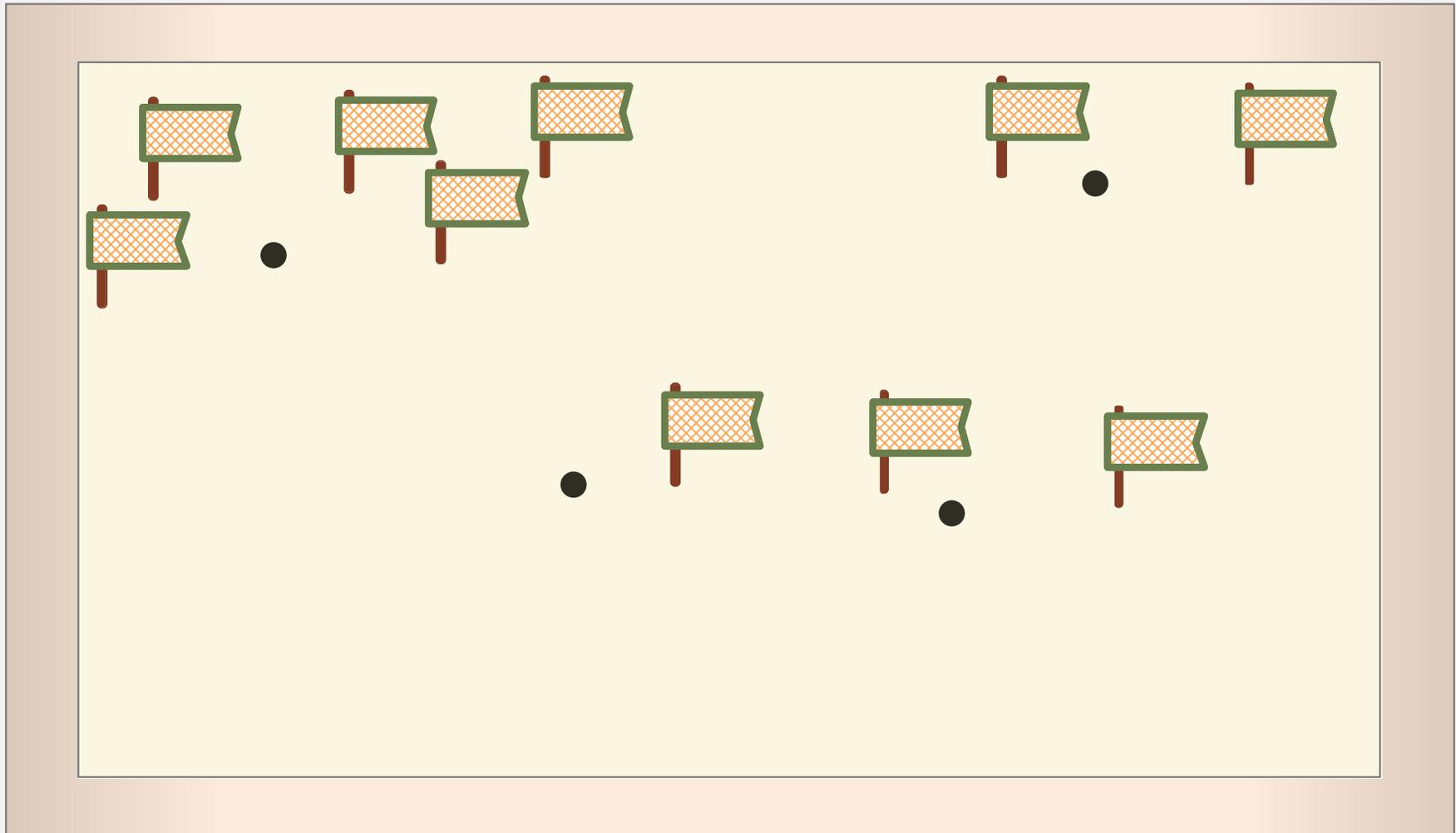
PHP  
+  
Hack

Python  
+  
Mypy

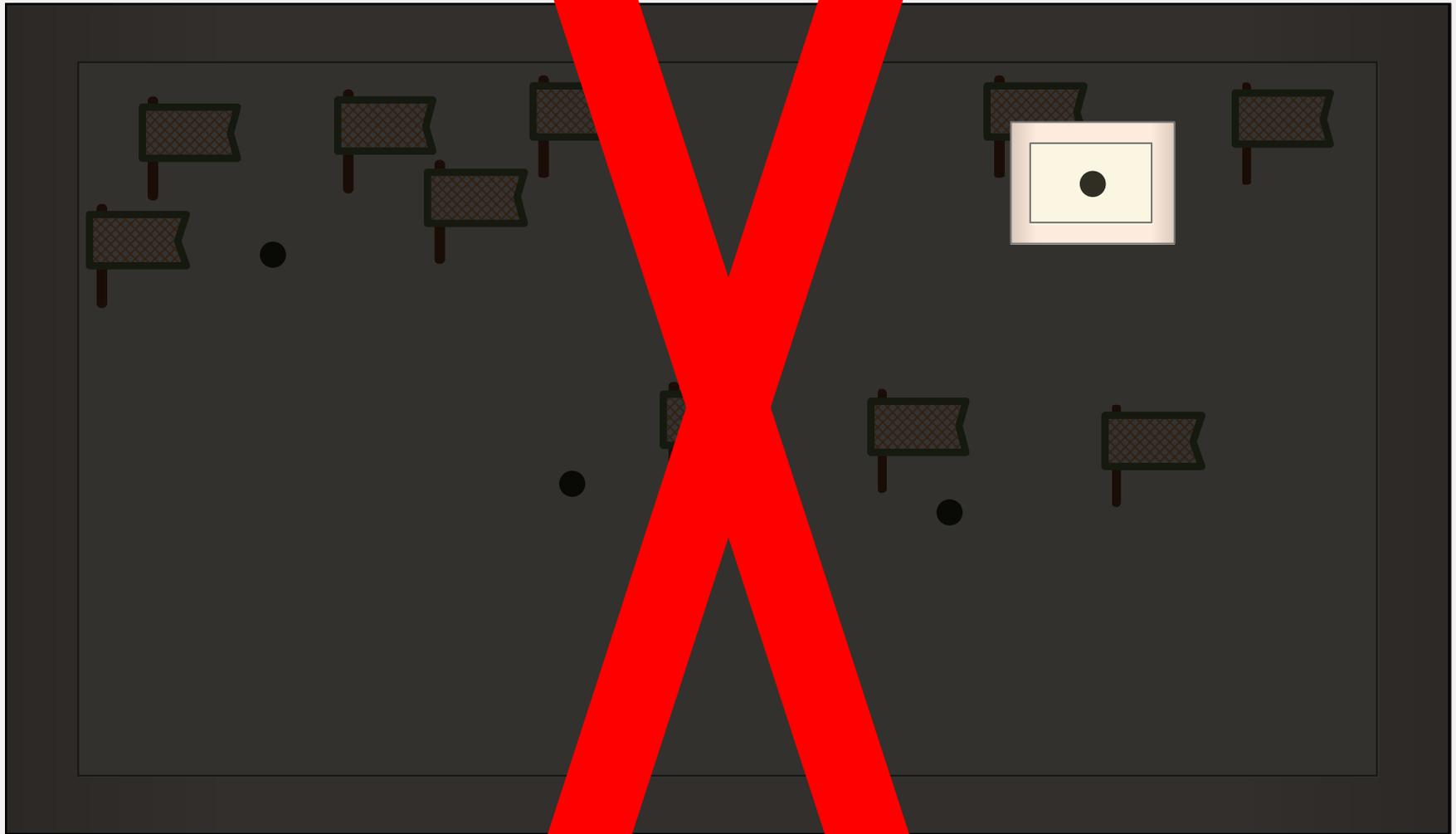
# Many Models, too

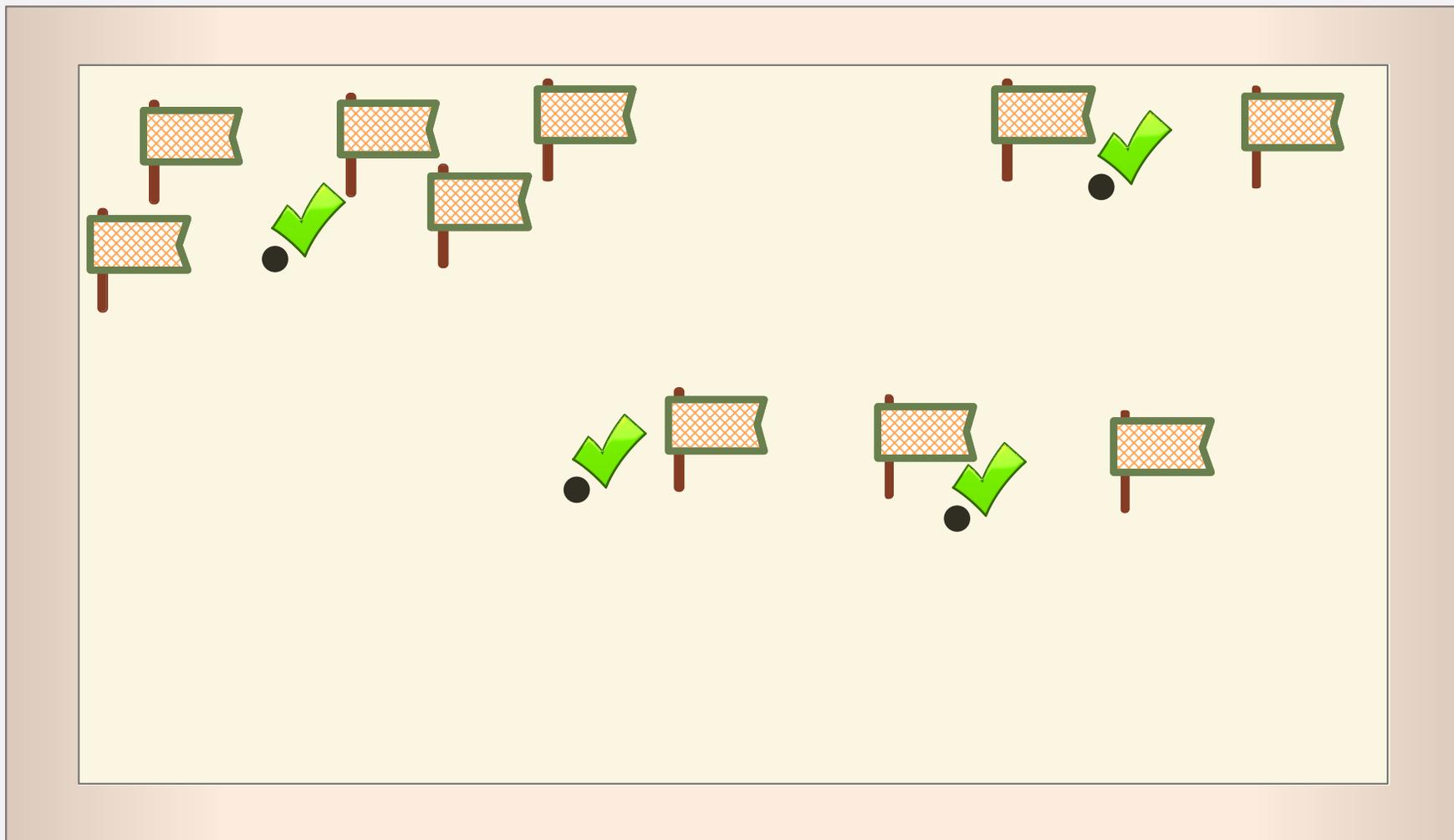


# Goal: Characterize the Landscape

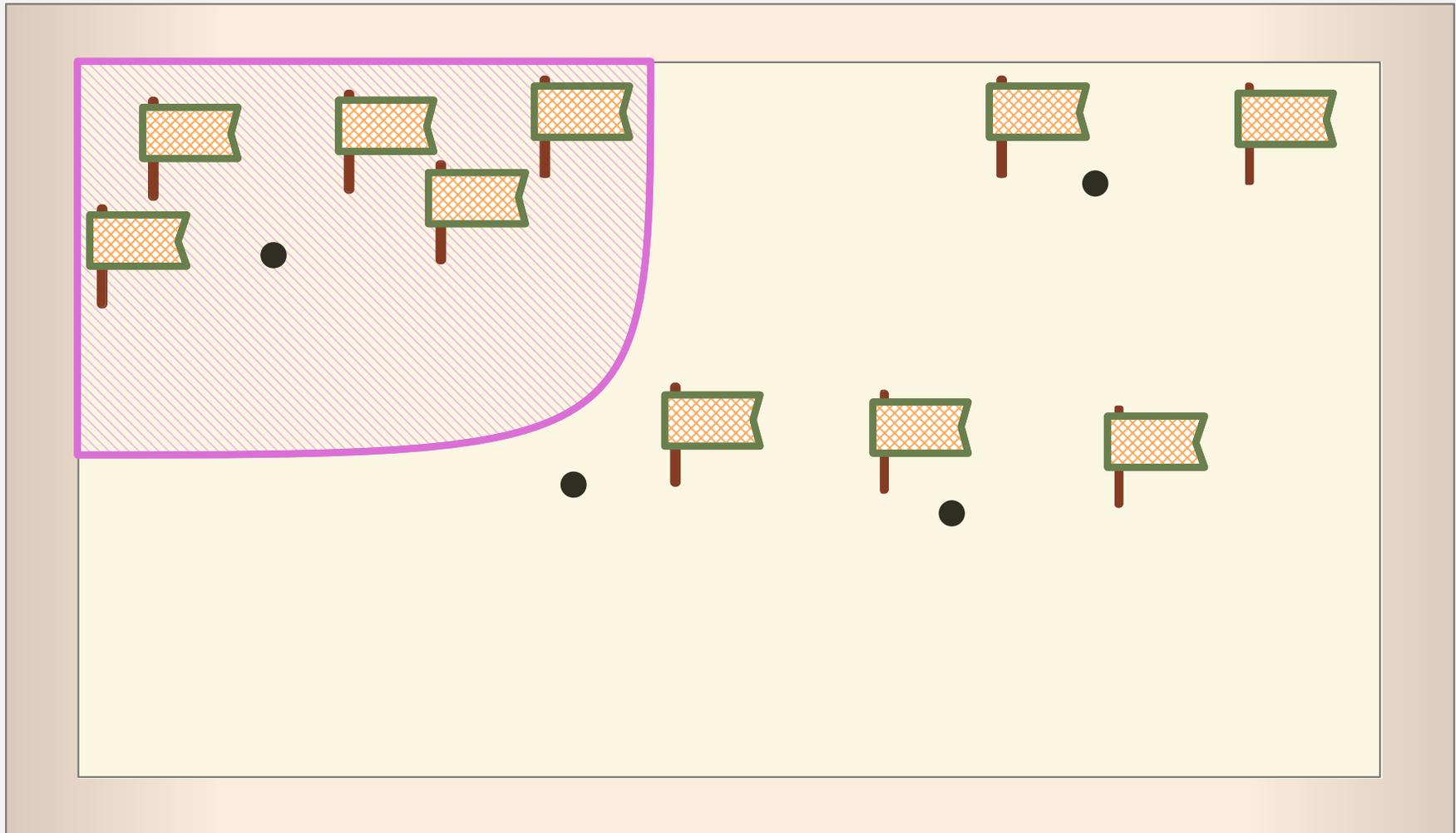


# Non-Goal: Restrict Landscape





# Warmup: Optional Typing / Erasure



# Example: Optional Typing

T

```
function f (x : [N,N]) {  
  ... fst x ...  
}
```

# Example: Optional Typing

T

```
function f (x : [N,N]) {  
  ... fst x ...  
}
```

U

```
f(9)
```

# Example: Optional Typing

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```
function f (x : [N,N]) {  
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```

Error: 9 is not a pair

U

f(9)

# Example: Optional Typing

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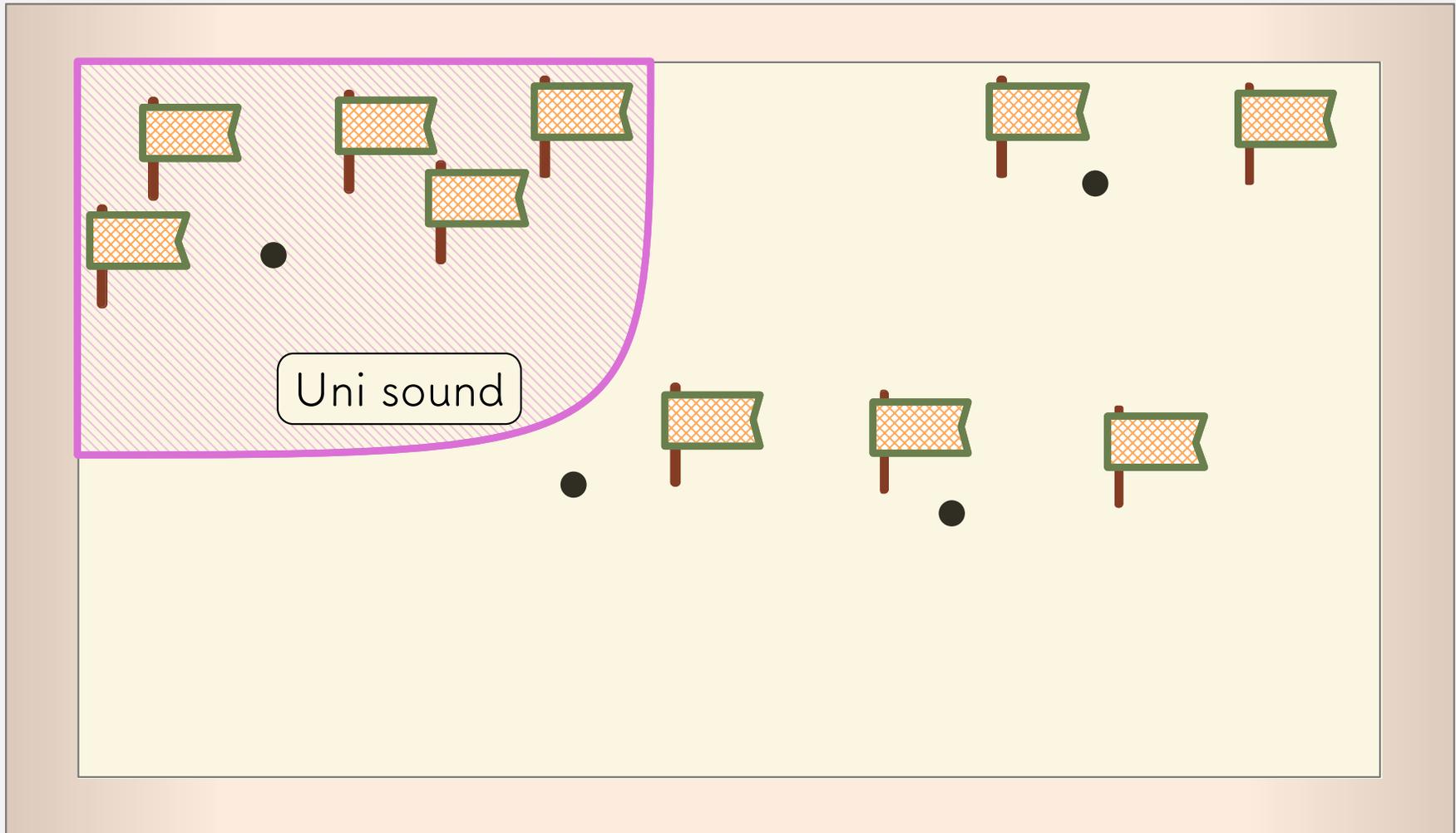
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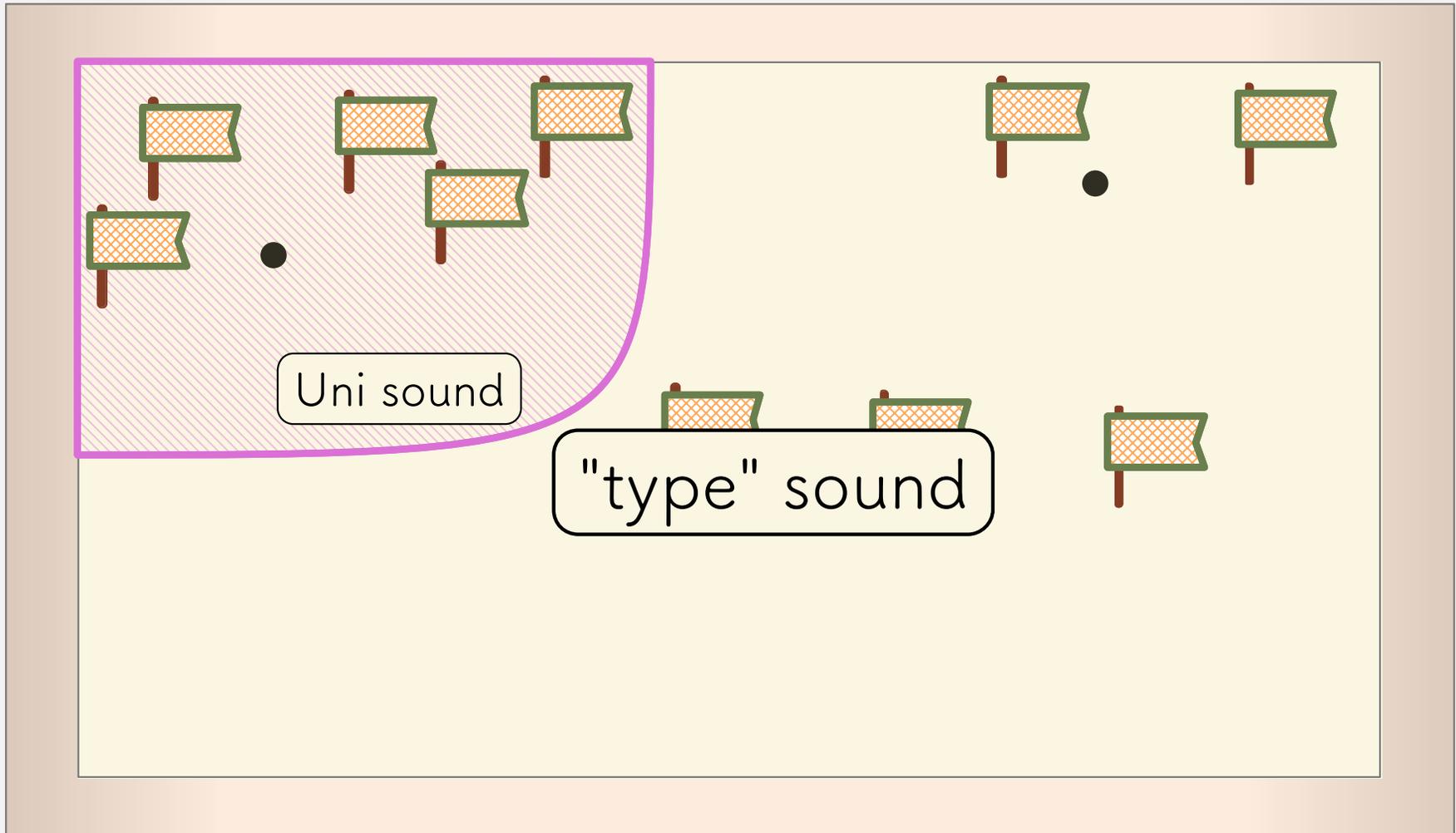
```
f(9)
```

types are **meaningless** at run-time  
**cannot help** debug a faulty program

 = Does Not Preserve Types



 = Does Not Preserve Types



ICFP '18

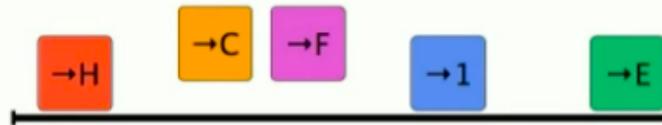
## A Spectrum of Type Soundness and Performance

Ben Greenman



Is type soundness all-or-nothing?

No! (in a mixed-typed language)



# ICFP '18 : Three Semantics, Soundnesses

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**Erase** semantics

- types predict nothing

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## **Transient** semantics

- types predict the top-level shape of values
- enforced by **tag checks**

# ICFP '18 : Three Semantics, Soundnesses

## **Erasure** semantics

- types predict nothing

## **Transient** semantics

- types predict the top-level shape of values
- enforced by **tag checks**

## **Natural** semantics

- types predict the full behavior of values
- enforced by higher-order **wrappers**

# ICFP '18 : Three Semantics, Soundnesses

**Erasure** semantics Uni sound

- types predict nothing

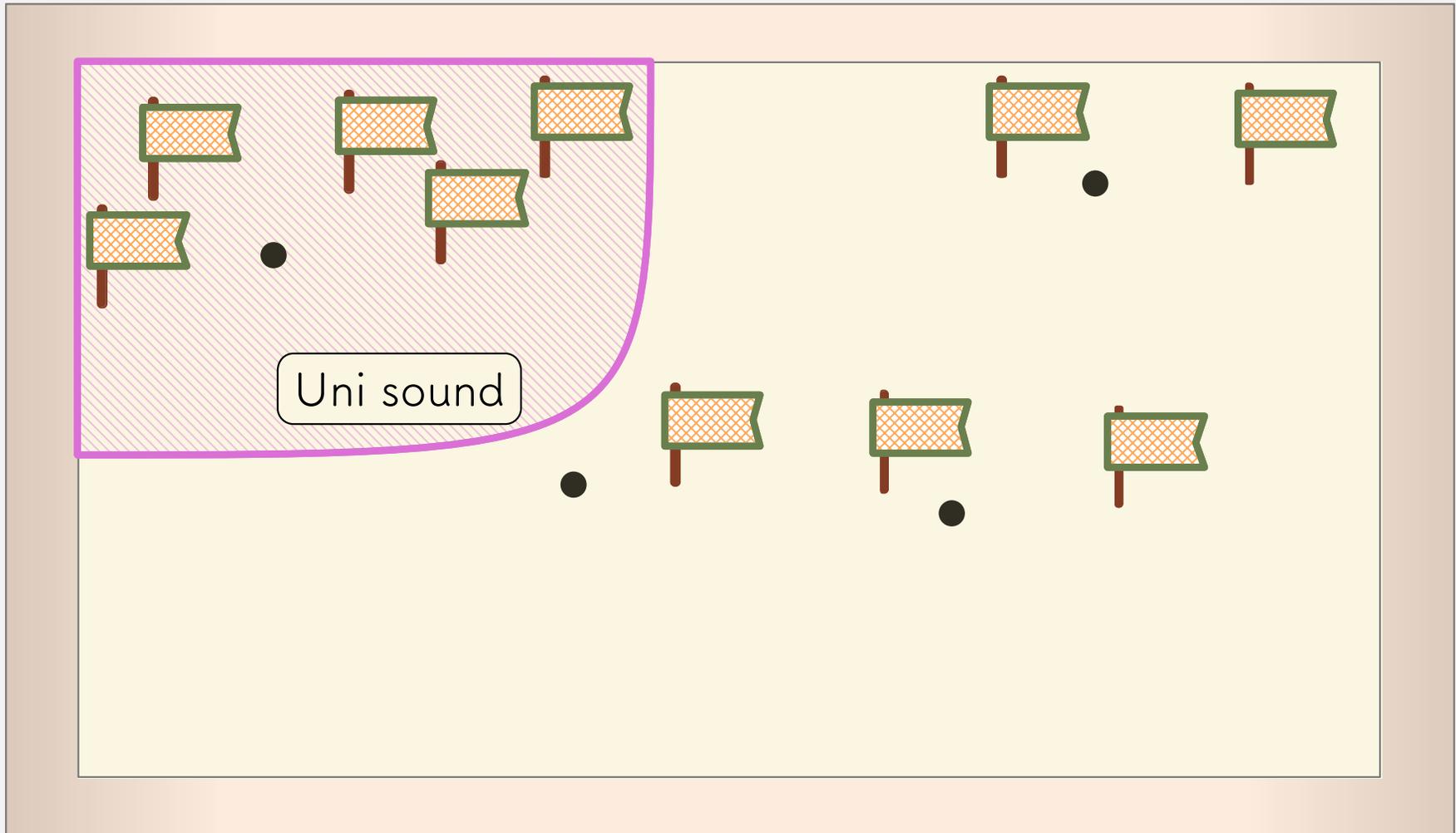
**Transient** semantics [T] sound

- types predict the top-level shape of values
- enforced by **tag checks**

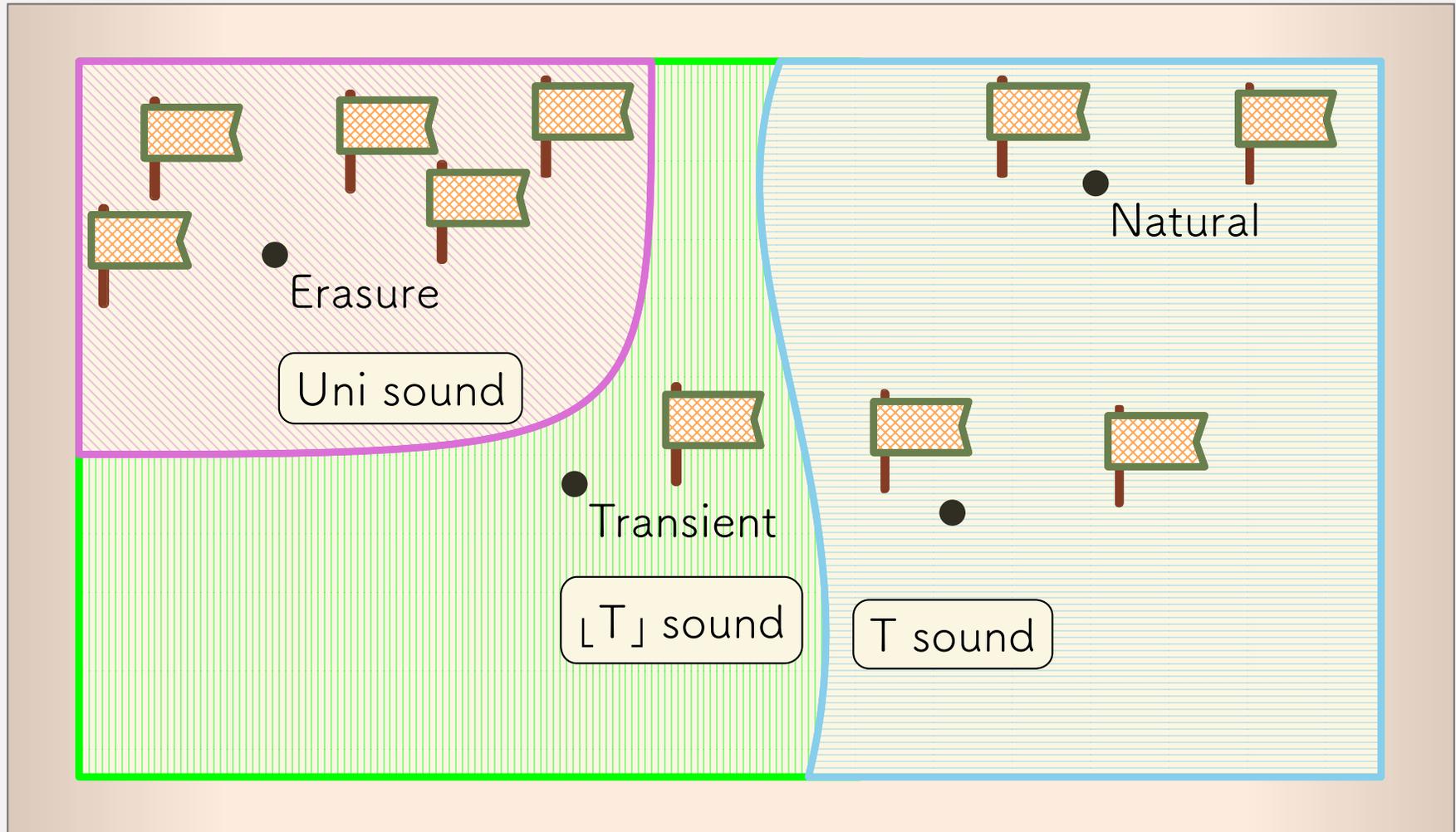
**Natural** semantics T sound

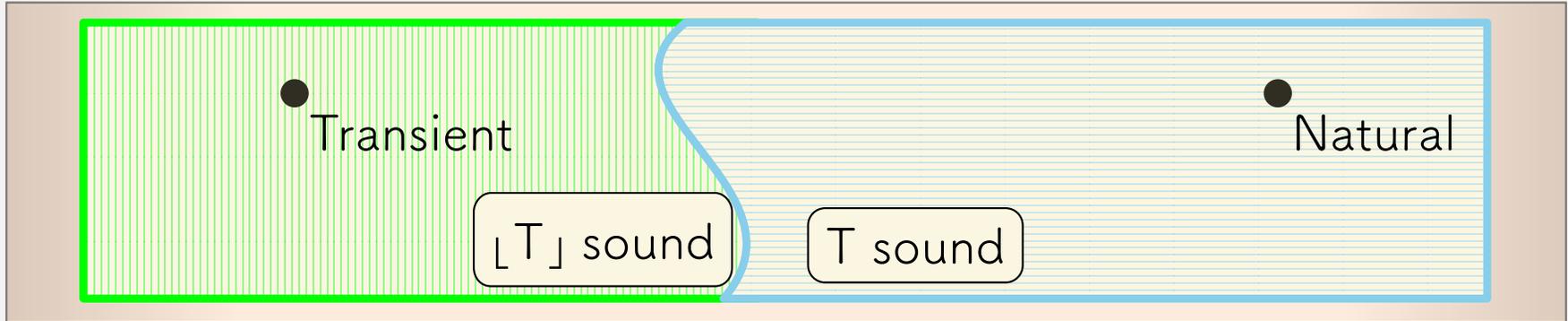
- types predict the full behavior of values
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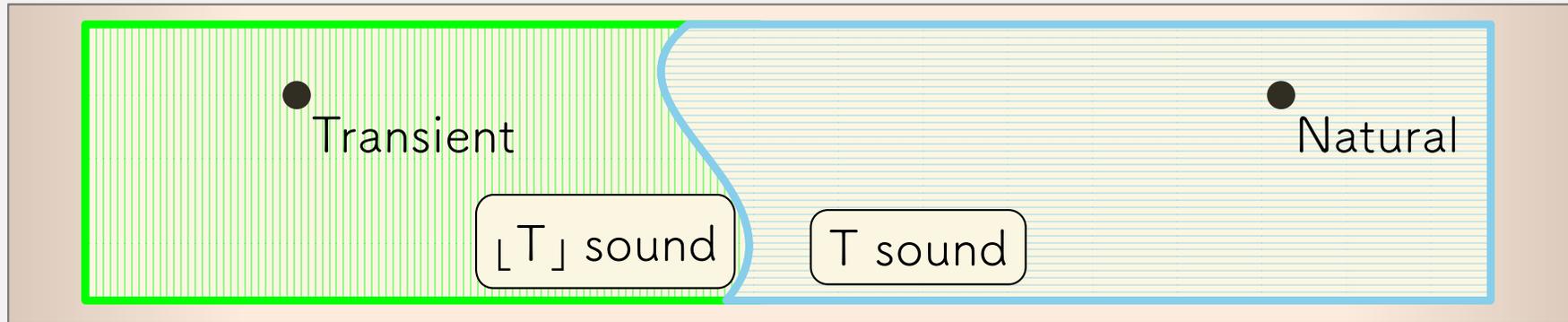
# ICFP '18: A Spectrum of Type Soundness



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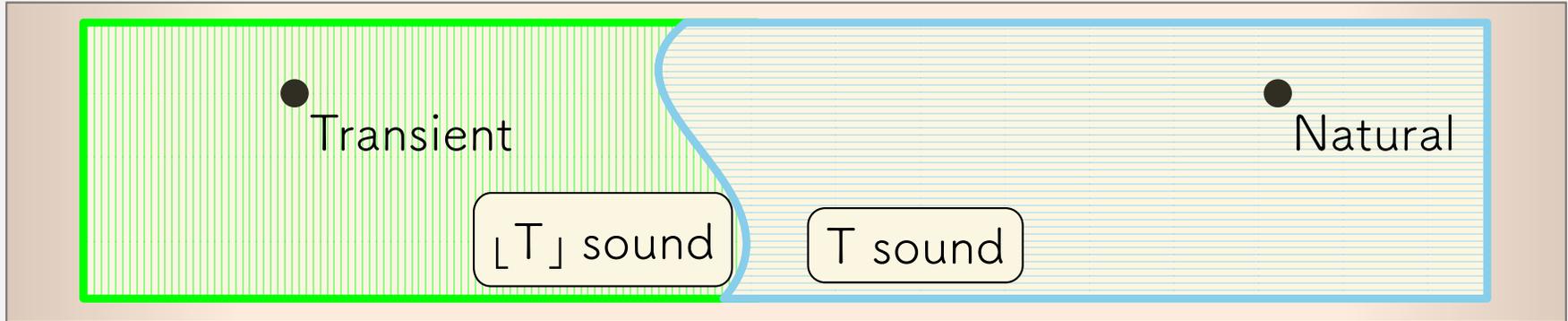


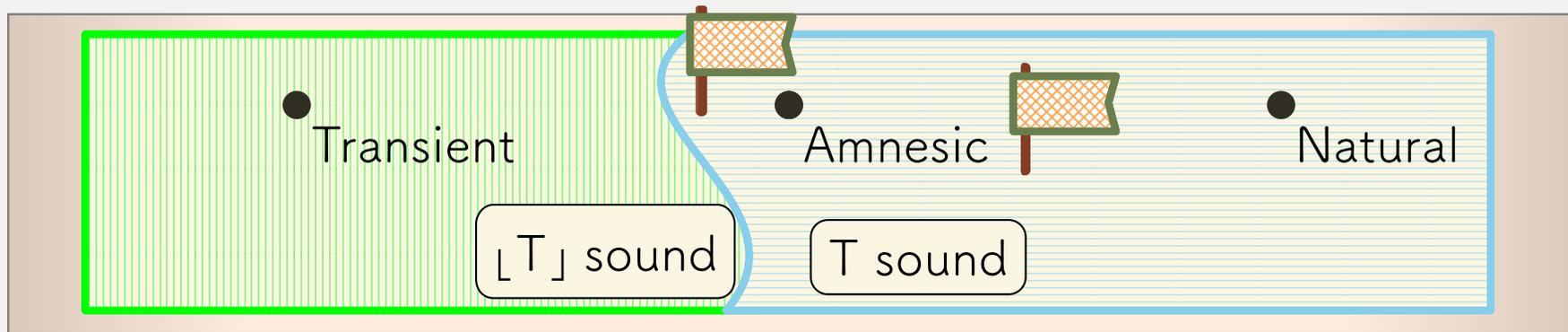
## Transient semantics └T┘ sound

- types predict the top-level shape of values
- enforced by **tag checks**

## Natural semantics T sound

- types predict the full behavior of values
- enforced by higher-order **wrappers**





OOPSLA '19

## Amnesic semantics

- enforce **tag checks**  $\lfloor T \rfloor$  with higher-order **wrappers**
- same behavior as Transient
- same type soundness as Natural

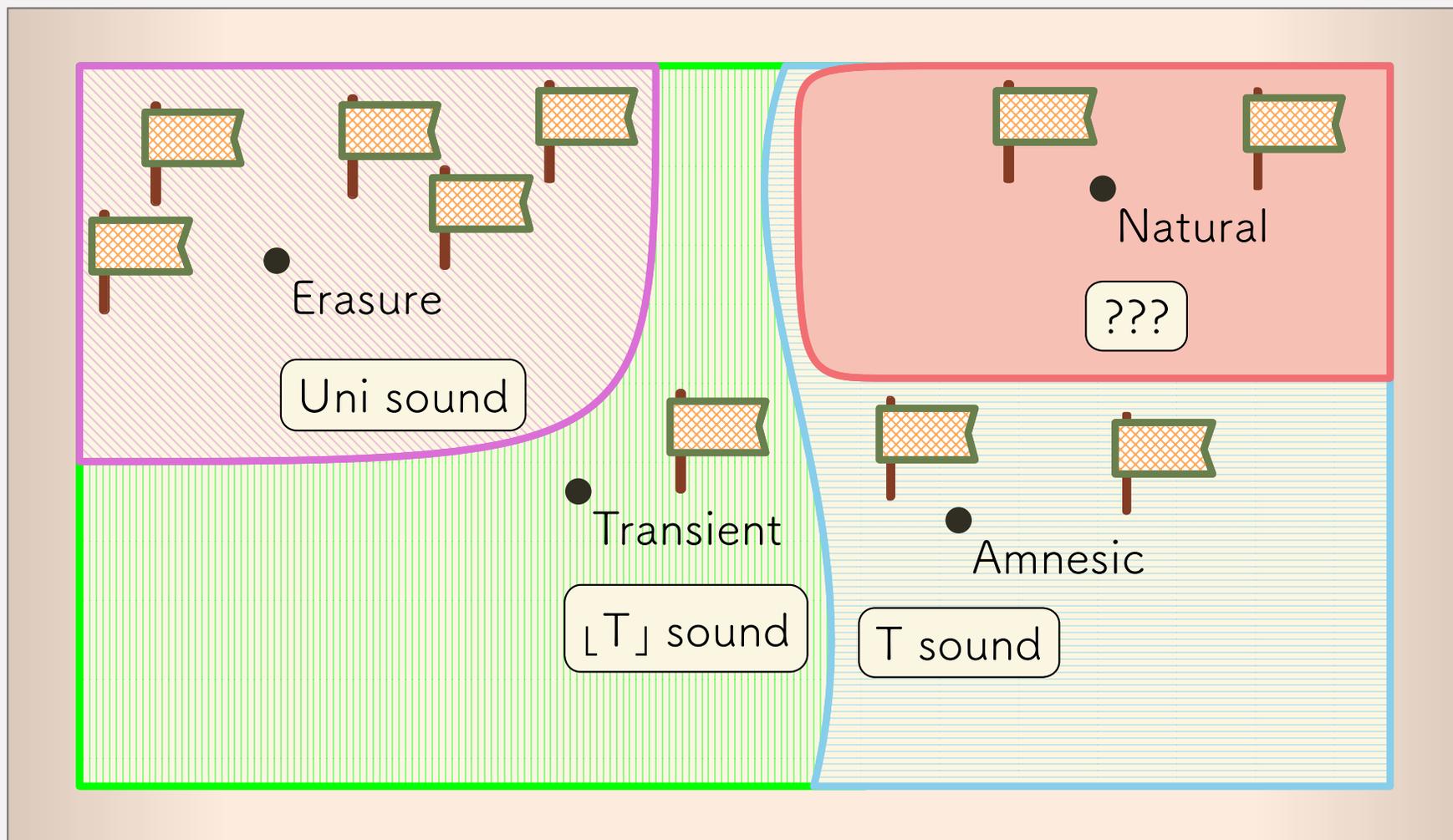


Greenberg POPL '15



Castagna, Lanvin ICFP '17

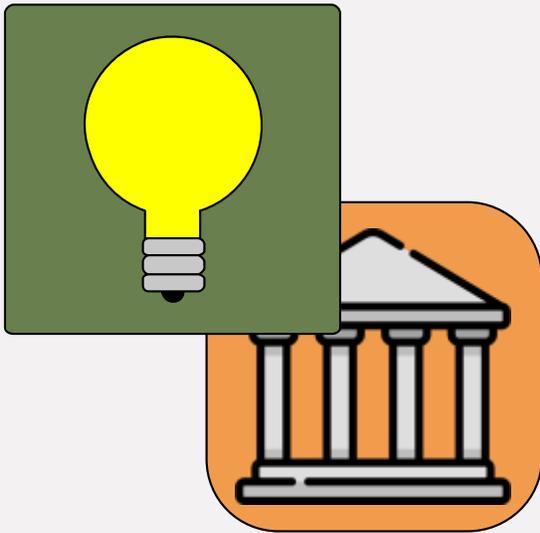
# Type Soundness is NOT ENOUGH



Example: Transient/Amnesic vs. Natural

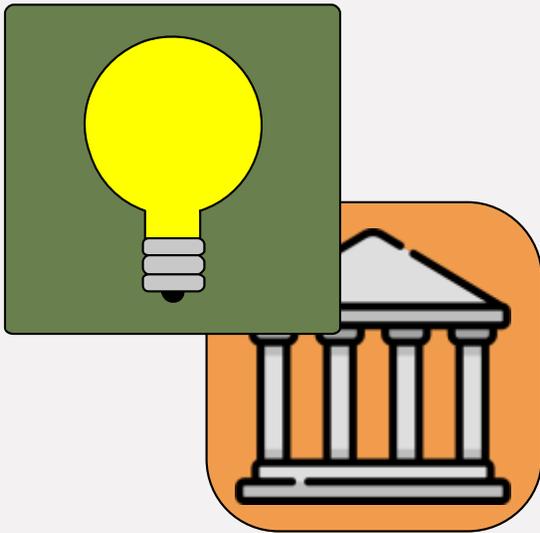
# Example: Transient/Amnesic vs. Natural

Prototyping



# Example: Transient/Amnesic vs. Natural

Prototyping



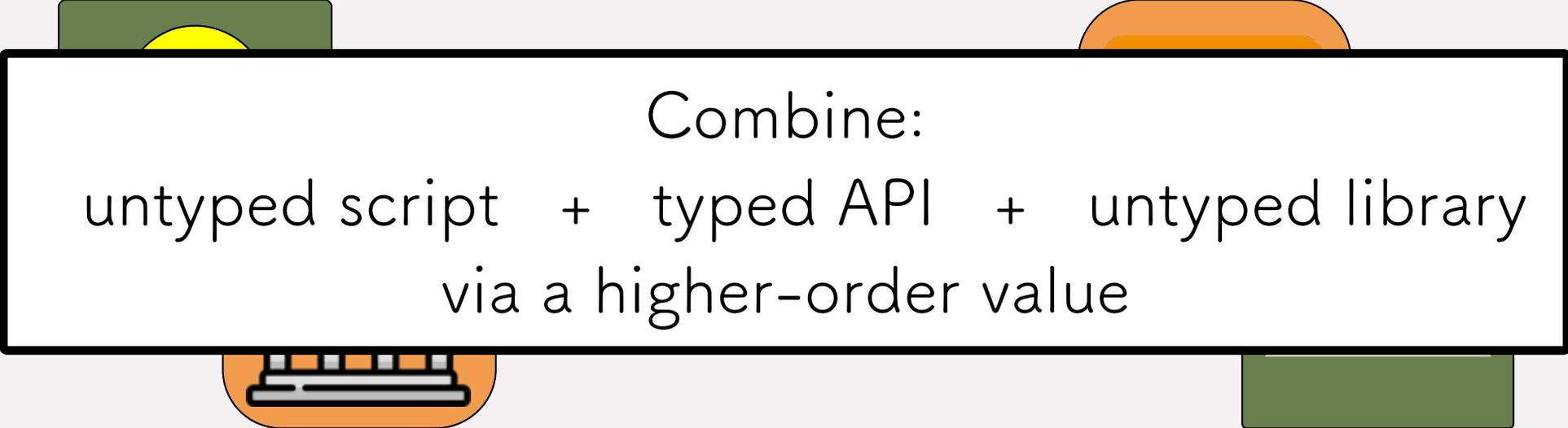
Library Re-Use



# Example: Transient/Amnesic vs. Natural

Prototyping

Library Re-Use

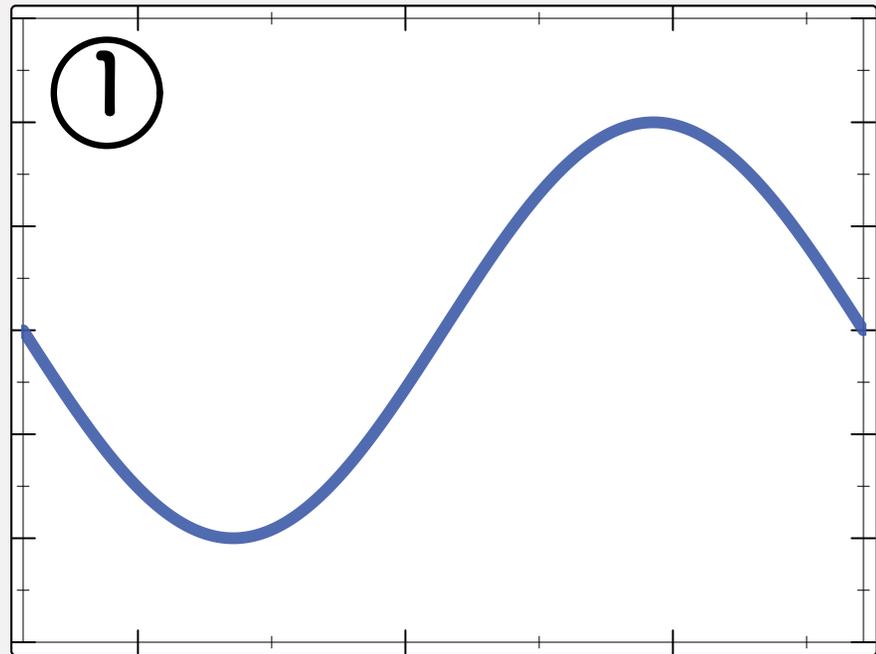


Combine:  
untyped script + typed API + untyped library  
via a higher-order value

# Example: Transient/Amnesic vs. Natural

## Clickable Plot

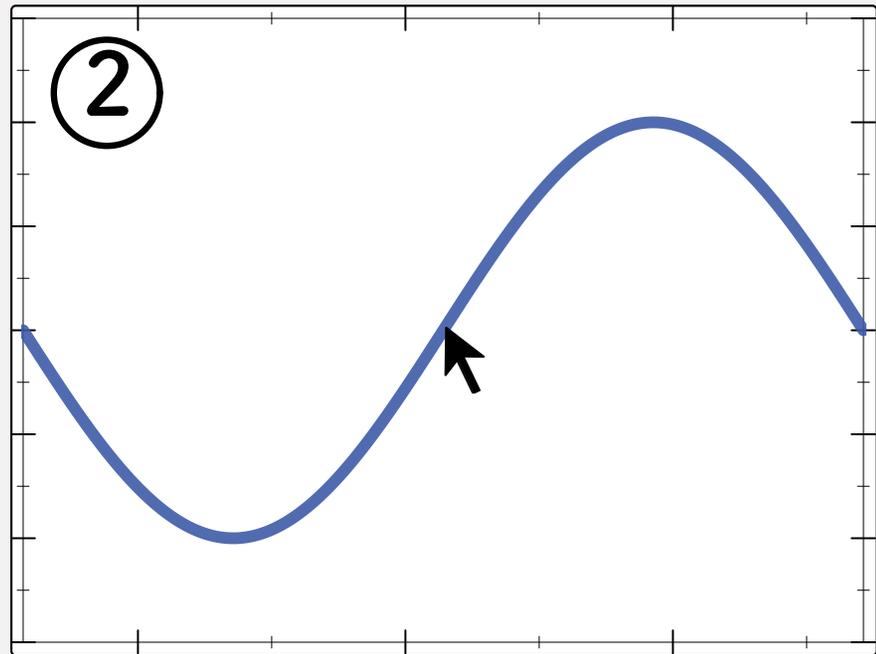
1. plot data
2. listen for a click
3. draw an image



# Example: Transient/Amnesic vs. Natural

## Clickable Plot

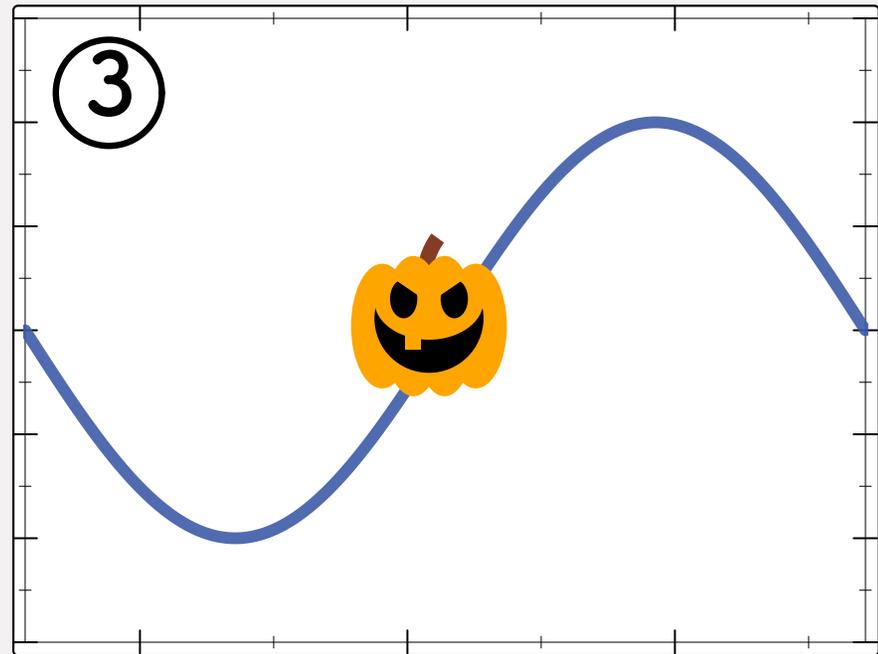
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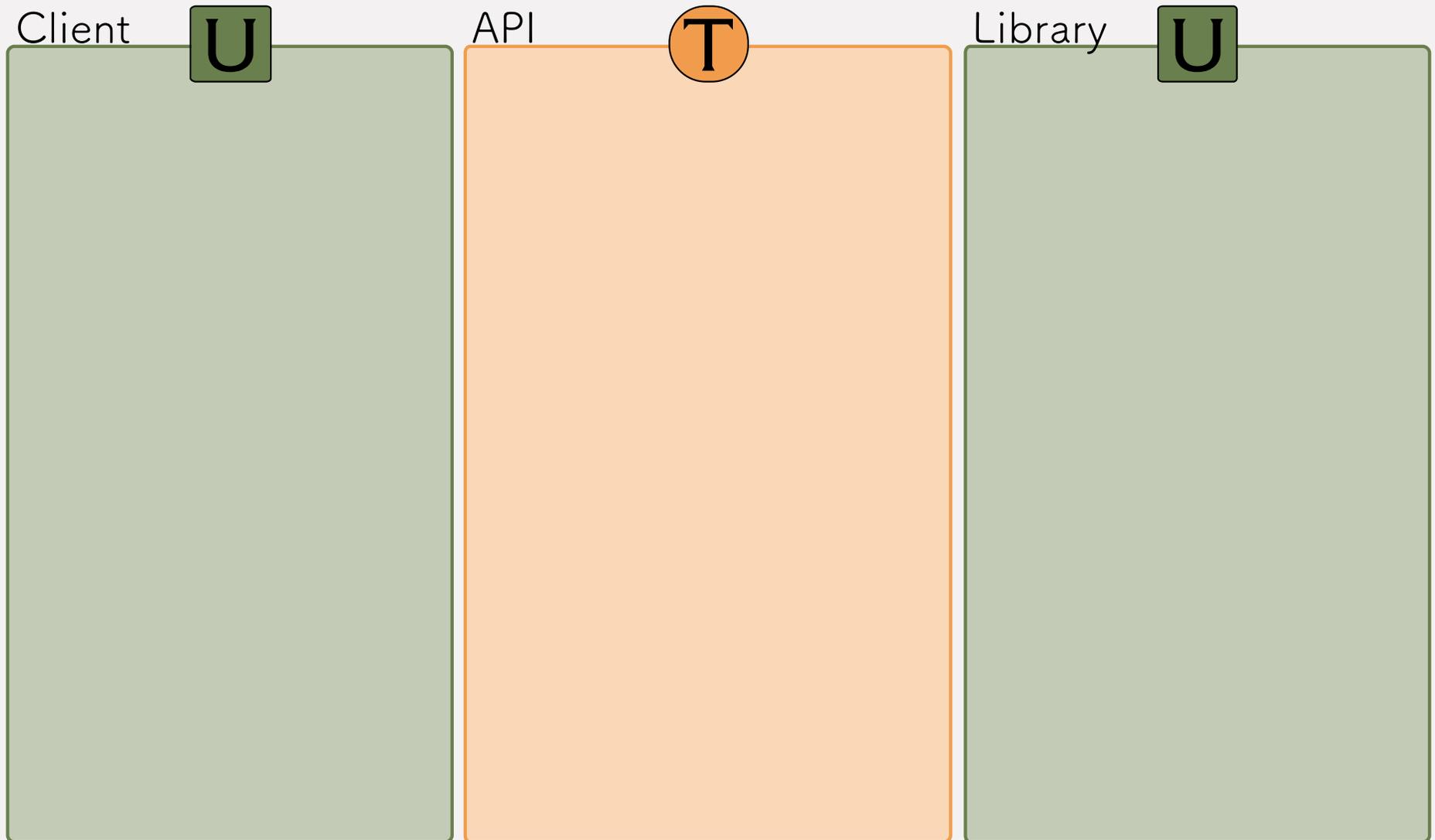
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1. plot data
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Clickable Plot



# Example: interactive plot



# Example: interactive plot

Client

U

```
function h(x) {  
  if (0 < fst x):  
    pumpkin  
  else:  
    fish  
}
```

```
p = ClickPlot(h)
```

```
p.show()
```

```
// click
```

API

T

Library

U

# Example: interactive plot

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    onClick){...}  
  
  mouseHandler(evt){  
    i = onClick(evt)  
    // draw i  
  }  
  
  show(){...}  
}
```

# Example: interactive plot

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API

**T**

```
type ClickPlot {  
  constructor(  
    ([N,N]) => Image)  
  
  mouseHandler :  
    (MouseEvent) => Void  
  
  show : () => Void  
}
```

Library

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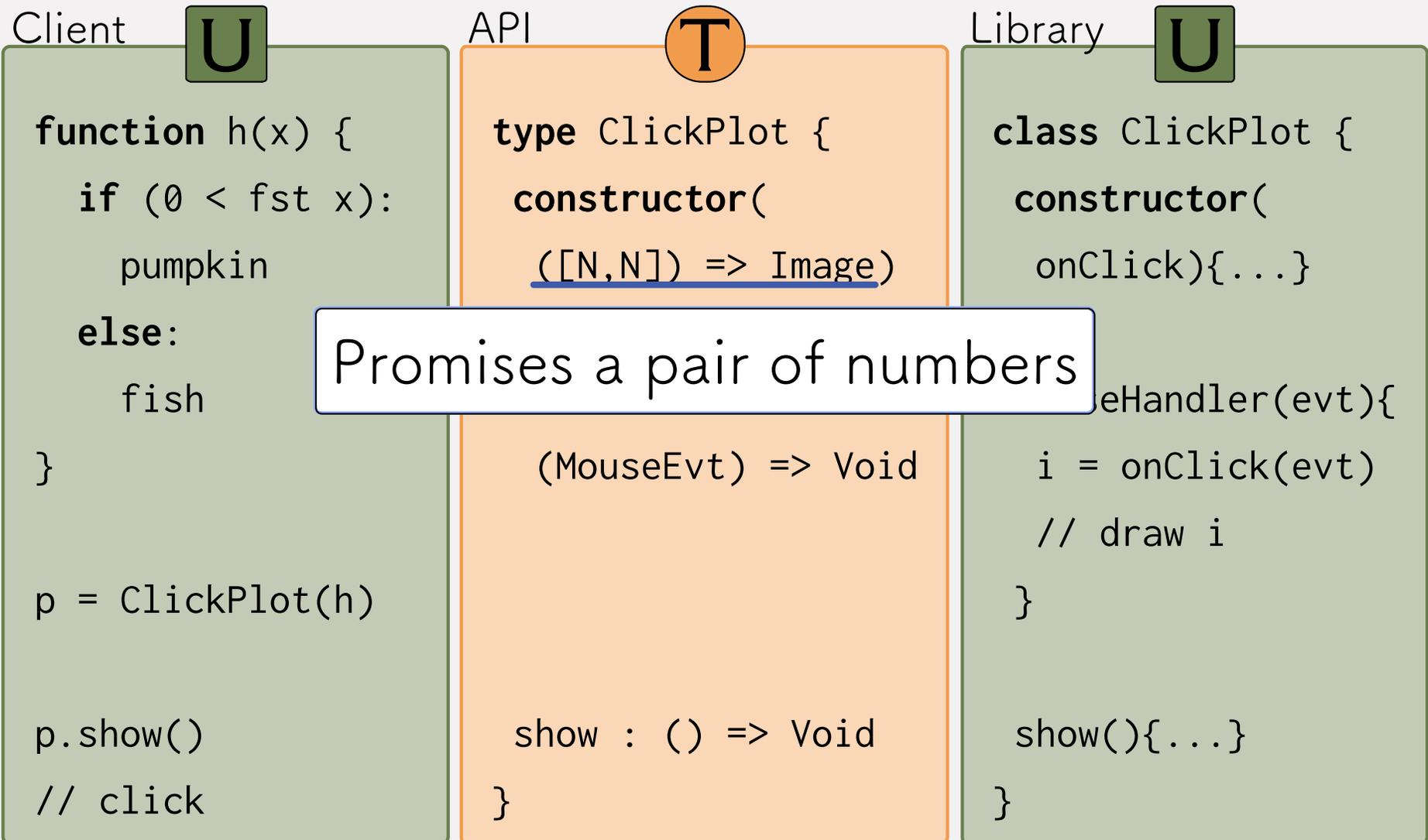
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}
```

Promises a pair of numbers

# Example: interactive plot

Client



```
function h(x) {
```

Expects a pair of numbers

```
  else:
```

```
    fish
```

```
}
```

```
p = ClickPlot(h)
```

```
p.show()
```

```
// click
```

API



```
type ClickPlot {
```

```
  or(
```

```
    => Image)
```

Promises a pair of numbers

```
(MouseEvent) => Void
```

```
  show : () => Void
```

```
}
```

Library



```
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```

```
  constructor(
```

```
    onClick){...}
```

```
  eHandler(evt){
```

```
    i = onClick(evt)
```

```
    // draw i
```

```
  }
```

```
  show(){...}
```

```
}
```

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```

Sends MouseEvent value

# Example: interactive plot

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type ClickPlot {  
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  (MouseEvent) => Void  
  
  show : () => Void  
}
```

[N,N] != MouseEvent

Sends MouseEvent value

Library

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```
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  mouseHandler(evt){  
    i = onClick(evt)  
  }  
  
  show(){...}  
}
```

# Example: interactive plot

Client

U

```
function h(x) {  
  if (0 < fst x):  
    pumpkin  
  else:  
    fish  
}
```

Q. Does h receive bad input?

```
p.show()  
// click
```

API

T

```
type ClickPlot {  
  constructor(  
    ([N,N]) => Image)
```

[N,N] != MouseEvent

```
(MouseEvent) => Void
```

```
show : () => Void  
}
```

Library

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```
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  mouseHandler(evt){  
    i = onClick(evt)
```

Sends MouseEvent value

```
show(){...}  
}
```

# Example: interactive plot

Client

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  }  
  
  show(){...}  
}
```

# Example: interactive plot

Client

**U**

```
function h(x) {  
  if (0 < fst x):
```

A. Yes, Trans/Amns

```
  else:
```

```
    fish
```

```
}
```

Q. Does h receive  
bad input?

```
p.show()
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```
// click
```

API

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```
type ClickPlot {  
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```

```
  mouse
```

```
  (Mo
```

A. No, Natural

```
  show : () => Void
```

```
}
```

Library

**U**

```
class ClickPlot {  
  constructor(  
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```

```
  mouseHandler(evt){
```

```
    i = onClick(evt)
```

```
    // draw i
```

```
}
```

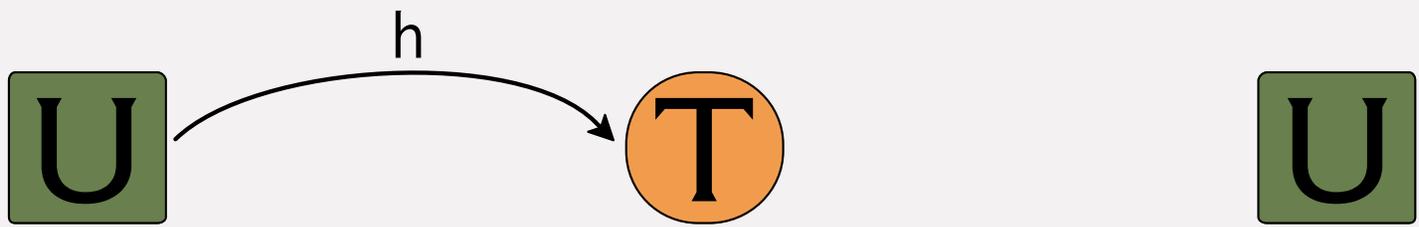
```
  show(){...}
```

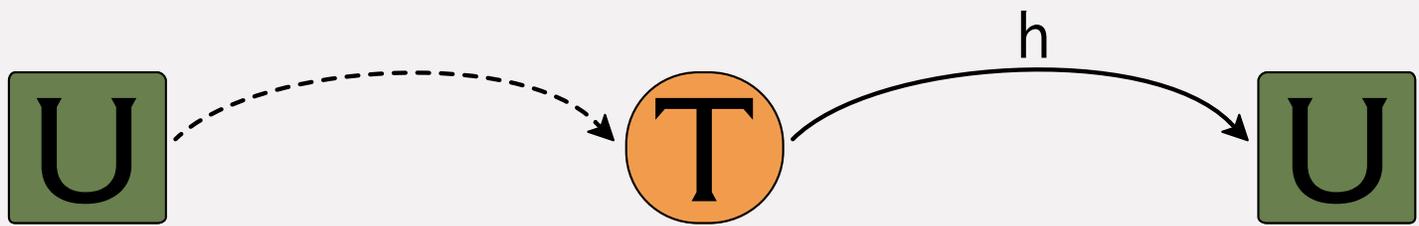
```
}
```

U

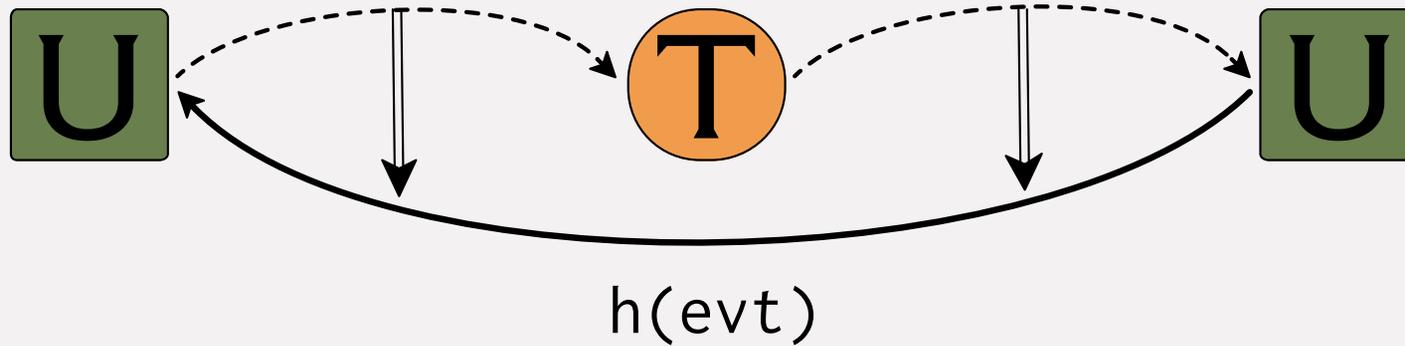
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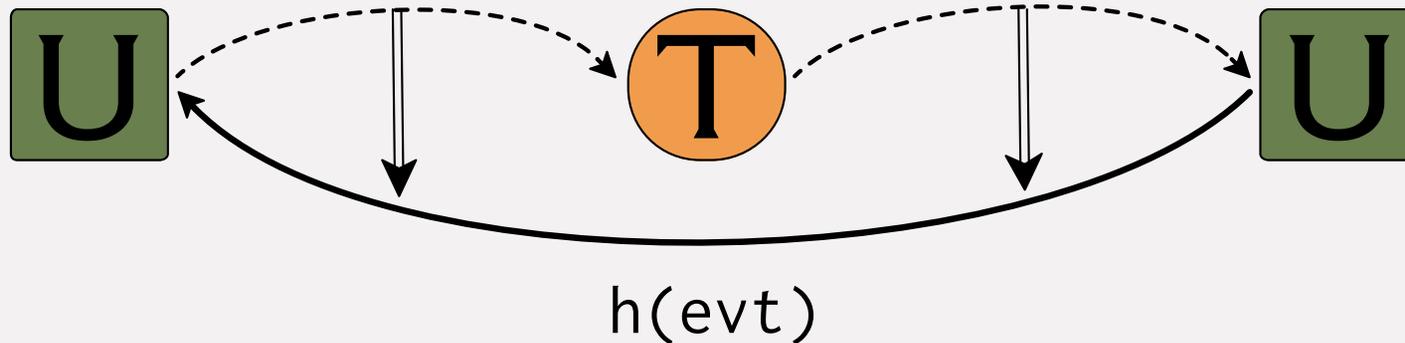




Q. Do types guard the **callback** channel?



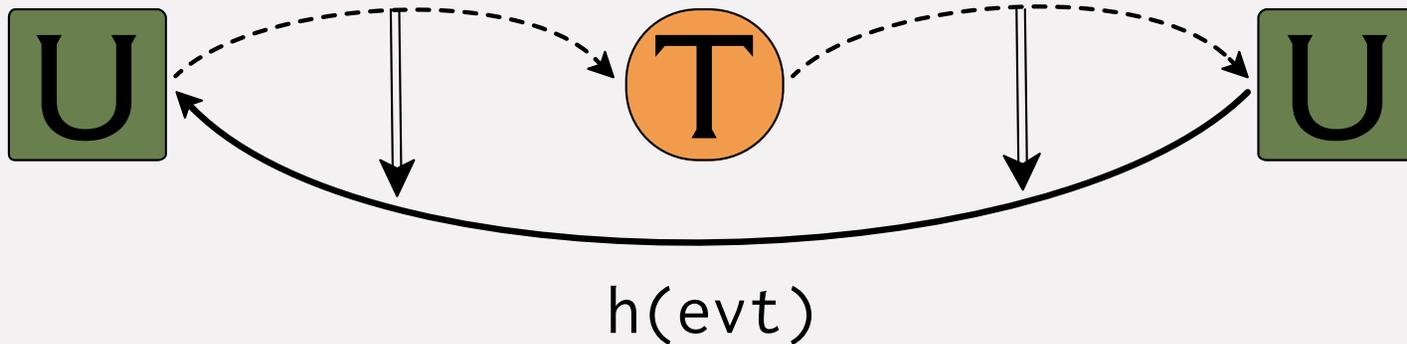
Q. Do types guard the **callback** channel?



**Transient/Amnesic:** no, because the channel is between two untyped components

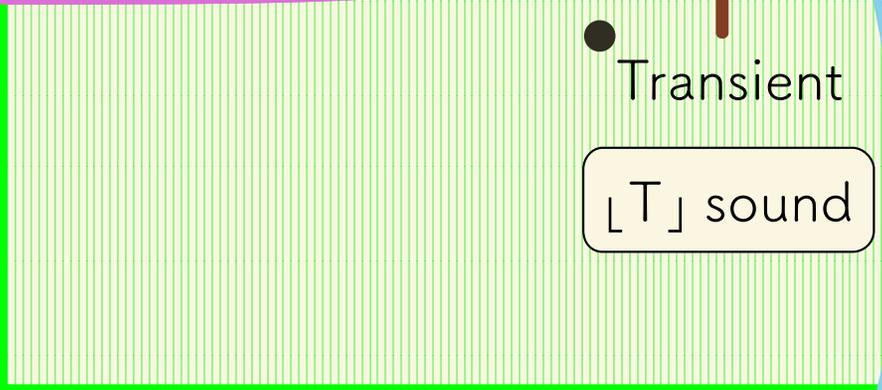
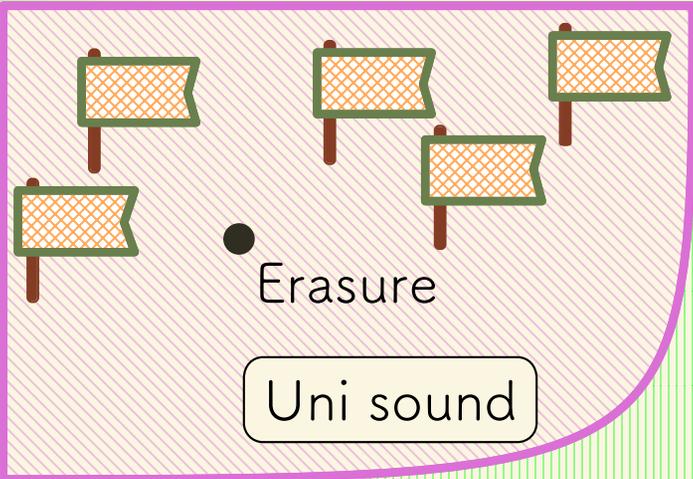
**Natural:** yes, because the channel was created via typed code

Q. Do types guard the **callback** channel?



Type Soundness  ~~$\Rightarrow$~~  yes

Complete Monitoring  $\Rightarrow$  yes



	Natural	Transient	Amnesic
type soundness	T	$\lfloor T \rfloor$	T
complete monitoring			

	Natural	Transient	Amnesic
type soundness	T	[T]	T
complete monitoring			
BLAME			

# Natural, Blame

Client

**U**

```
function h(x) {  
  if (0 < fst x):  
    pumpkin  
  else:  
    fish  
}  
  
p = ClickPlot(h)  
  
p.show()  
// click
```

API

**T**

```
type ClickPlot {  
  constructor(  
    ([N,N]) => Image)  
  
  mouseHandler :  
    (MouseEvent) => Void  
  
  show : () => Void  
}
```

Library

**U**

```
class ClickPlot {  
  constructor(  
    onClick){...}  
  
  mouseHandler(evt){  
    i = onClick(evt)  
    // draw i  
  }  
  
  show(){...}  
}
```

# Natural, Blame

Client

**U**

```
function h(x) {  
  if (0 < fst x):  
    pumpkin  
  else:  
    fish  
}  
  
p = ClickPlot(h)  
  
p.show()  
// click
```

API

**T**

```
type ClickPlot {  
  constructor(  
    ([N,N]) => Image)  
  mouseHandler(  
    (Image) => Image)  
  show : () => Void  
}
```

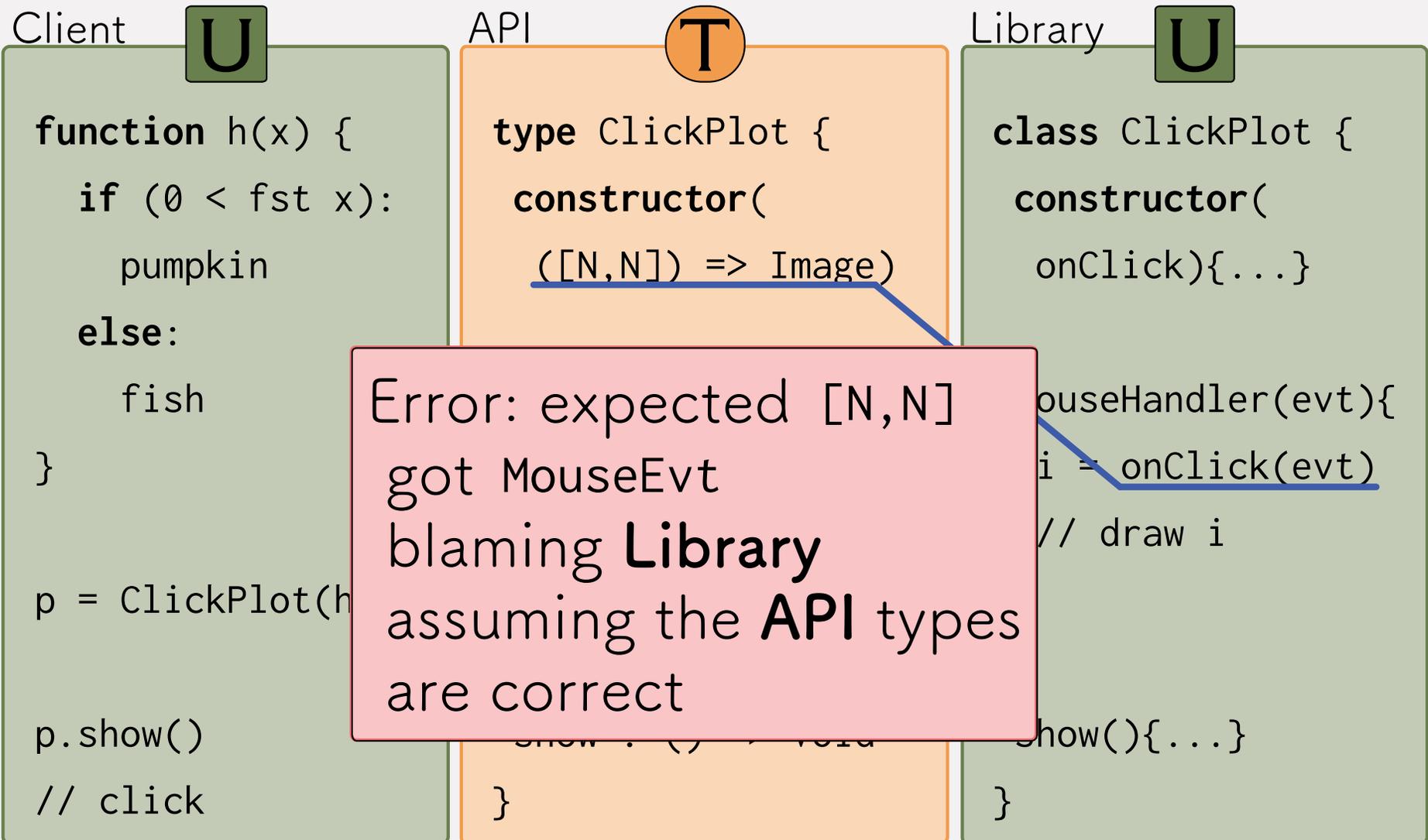
Library

**U**

```
class ClickPlot {  
  constructor(  
    onClick){...}  
  mouseHandler(evt){  
    i = onClick(evt)  
    // draw i  
  }  
  show(){...}  
}
```

Error: MouseEvt  
is not a pair

# Natural, Blame



# Transient/Amnesic, Blame

Client

**U**

```
function h(x) {  
  if (0 < fst x):  
    pumpkin  
  else:  
    fish  
}  
  
p = ClickPlot(h)  
  
p.show()  
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API

**T**

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type ClickPlot {  
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Library

**U**

```
class ClickPlot {  
  constructor(  
    onClick){...}  
  
  mouseHandler(evt){  
    i = onClick(evt)  
    // draw i  
  }  
  
  show(){...}  
}
```

# Transient/Amnesic, Blame

Client

**U**

```
function h(x) {  
  if (0 < fst x):
```

Error: <obj>  
is not a pair  
blaming:

**Client / API**  
**API / Library**

```
p.show()  
// click
```

API

**T**

```
type ClickPlot {  
  constructor(  
    ([N,N]) => Image)
```

```
  mouseHandler :  
    (MouseEvent) => Void
```

```
  show : () => Void  
}
```

Library

**U**

```
class ClickPlot {  
  constructor(  
    onClick){...}
```

```
  mouseHandler(evt){  
    i = onClick(evt)  
    // draw i  
  }
```

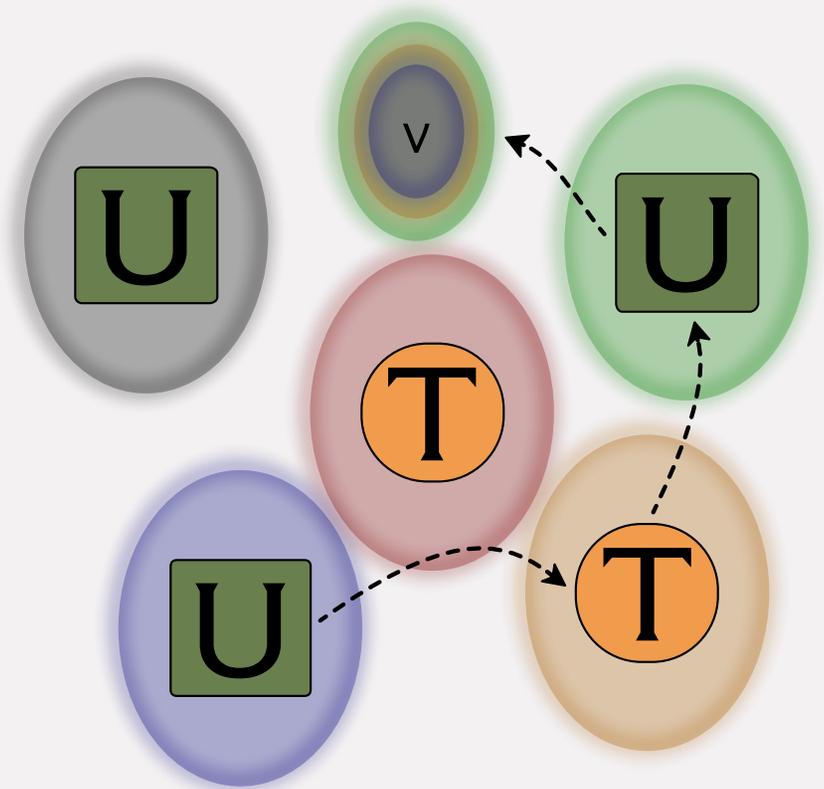
```
  show(){...}  
}
```

# Blame Properties

1. blame **only**  
responsible edges

2. blame **all**  
responsible edges

3. blame **exactly** the responsible edges



# Blame Properties

Blame Soundness

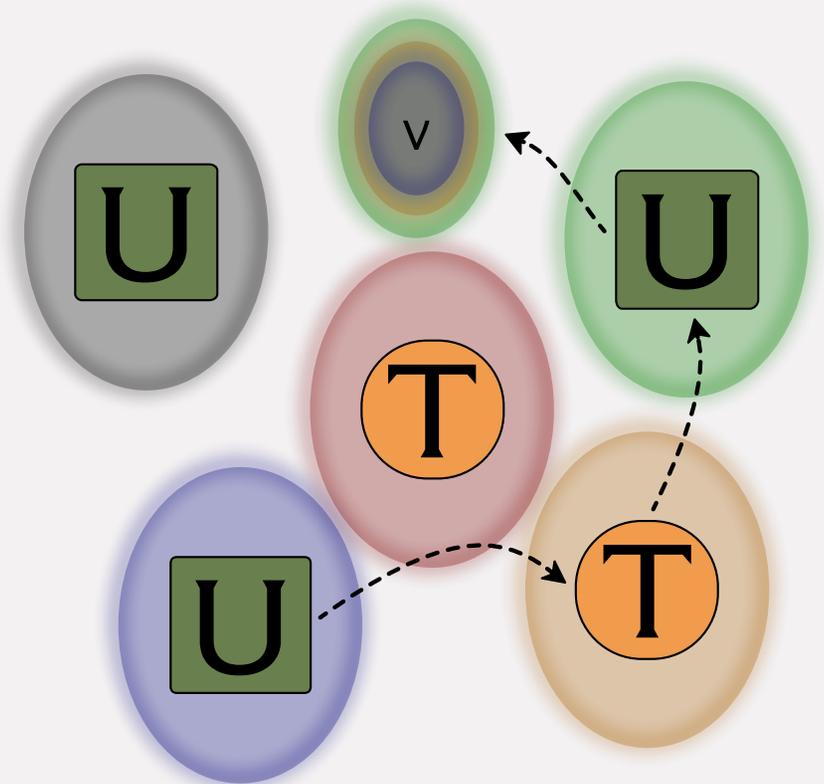
1. blame **only**  
responsible edges

Blame Completeness

2. blame **all**  
responsible edges

B. Soundness + B. Completeness

3. blame **exactly** the responsible edges



	Natural	Transient	Amnesic
type soundness	T	[T]	T
complete monitoring	✓	✗	✗
blame soundness	✓		
blame completeness	✓		

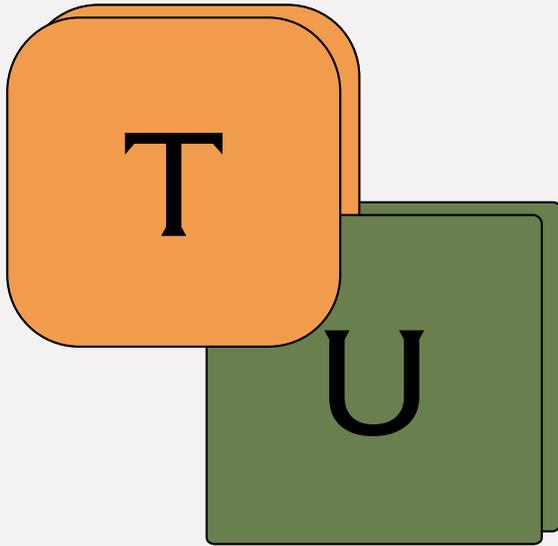
	Natural	Transient	Amnesic
type soundness	T	[T]	T
complete monitoring	✓	✗	✗
blame soundness	✓	✗	✓
blame completeness	✓	✗	✓

# Every Typed Language is Mixed-Typed



Many typed languages  
**trust** untyped code

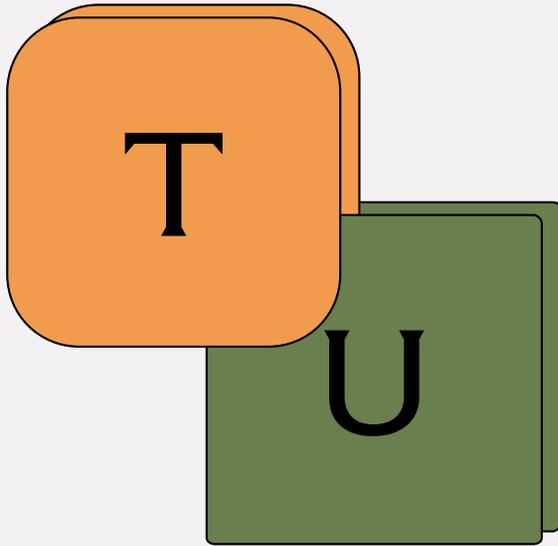
# Every Typed Language is Mixed-Typed



Many typed languages  
**trust** untyped code

Gradual typing makes these  
boundaries **visible** ...

# Every Typed Language is Mixed-Typed



Many typed languages  
**trust** untyped code

Gradual typing makes these  
boundaries **visible** ...

... and **challenges** our notions of types and  
what types mean

Complete monitoring **strengthens** type soundness  
for programs that **compose** typed and untyped

and **enables** precise statements about  
the quality of blame

Code + Proofs:

[github.com/nuprl/gfd-oopsla-2019](https://github.com/nuprl/gfd-oopsla-2019)

	Natural	Transient	Amnesic
type soundness	T	[T]	T
complete monitoring*	✓	✗	✗
blame soundness*	✓	✗	✓
blame completeness*	✓	✗	✓

