

MSDscript

```
_let x = 3  
_in x
```

➡ 3

MSDscript with Conditionals

```
_let x = 3
_in  _if x == 3
      _then 1
      _else 0
```

MSDscript with Conditionals

```
new: _if ... _then ... _else  
_let x = 3  
_in _if x == 3  
    _then 1  
    _else 0
```

MSDscript with Conditionals

```
_let x = 3  
_in  _if x == 3  
      _then 1  
      _else 0
```

also new: ==

MSDscript with Conditionals

```
_let x = 3  
_in  _if x == 3  
      _then 1  
      _else 0
```

➡ 1

MSDscript with Conditionals

```
_let x = 3
_in  _if x == 3
      _then 1
      _else 0
```

_if and == always together?

➡ 1

MSDscript with Conditionals

```
_let x = 3
_in  _let same = (x == 3)
      _in _if same
          _then 1
          _else 0
```

MSDscript with Conditionals

```
_let x = 3
_in _let same = (x == 3)
    _in _if same
        _then 1
        _else 0
```

== is a new kind of expression

MSDscript with Conditionals

```
_let x = 3
_in _let same = _if <expr> _then <expr> _else
_in _if same
    _then 1
    _else 0
```

MSDscript with Conditionals

```
_let x = 3
_in _let same = (x == 3)
    _in _if same
        _then 1
        _else 0
```

➡ 1

MSDscript with Conditionals

```
1 + (_if 3 == 3
      _then 1
      _else 0)
```

➡ 2

MSDscript with Conditionals

```
1 + (_if 3 == 3  
      _then 1  
      _else 0)
```

Like
(... ? ... : ...)
in C-style languages

➡ 2

MSDscript Expressions and Values

`(1 + 2) == 3`

➡ `_true`

MSDscript Expressions and Values

`(1 + 2) == 3`

➡ `_true`

New kind of **value**

`(1 + 2) == 3` is an **expression**

An expression has a **value** as determined by `interp`

The value of `(1 + 2) == 3` is `_true`

MSDscript Expressions and Values

`(1 + 2) == 3`

➡ `_true`

New kind of **value**

`1 + 2` is an **expression**

An expression has a **value** as determined by `interp`

The value of `1 + 2` is 3

MSDscript Expressions and Values

`(1 + 2) == 3`

➡ `_true`

New kind of **value**

Some expressions look the same as their values

3 is an **expression**

It has the **value** 3

MSDscript Expressions and Values

`(1 + 2) == 3`

➔ `_true`

New kind of **value**

For now, let's have an expression for each value

`_true` is an **expression**

It has the **value** `_true`

MSDscript Expressions and Values

```
_if _true  
_then 1  
_else 0
```

➡ 1

MSDscript Expressions and Values

`(1 + 2) == 0`

➡ `_false`

MSDscript with Booleans

$\langle \text{expr} \rangle$ = $\langle \text{number} \rangle$
| $\langle \text{boolean} \rangle$ 
| $\langle \text{expr} \rangle$ **==** $\langle \text{expr} \rangle$ 
| $\langle \text{expr} \rangle$ **+** $\langle \text{expr} \rangle$
| $\langle \text{expr} \rangle$ ***** $\langle \text{expr} \rangle$
| $\langle \text{variable} \rangle$
| **_let** $\langle \text{variable} \rangle$ **=** $\langle \text{expr} \rangle$ **_in** $\langle \text{expr} \rangle$
| **_if** $\langle \text{expr} \rangle$ **_then** $\langle \text{expr} \rangle$ **_else** $\langle \text{expr} \rangle$ 

 $\langle \text{val} \rangle$ = $\langle \text{number} \rangle$
| $\langle \text{boolean} \rangle$ 

MSDscript with Booleans

$\langle \text{expr} \rangle$ = $\langle \text{number} \rangle$
| $\langle \text{boolean} \rangle$ 
| $\langle \text{expr} \rangle == \langle \text{expr} \rangle$ 
| $\langle \text{expr} \rangle + \langle \text{expr} \rangle$
| $\langle \text{expr} \rangle * \langle \text{expr} \rangle$
| $\langle \text{variable} \rangle$
| `_let` $\langle \text{variable} \rangle = \langle \text{expr} \rangle$ `_in` $\langle \text{expr} \rangle$
| `_if` $\langle \text{expr} \rangle$ `_then` $\langle \text{expr} \rangle$ `_else` $\langle \text{expr} \rangle$ 

$\langle \text{val} \rangle$ = $\langle \text{number} \rangle$
| $\langle \text{boolean} \rangle$ 

$\langle \text{boolean} \rangle$ = `_true`
| `_false`

MSDscript with Booleans

$\langle \text{expr} \rangle$ = $\langle \text{number} \rangle$
| $\langle \text{boolean} \rangle$
| $\langle \text{expr} \rangle == \langle \text{expr} \rangle$ lower precedence than + or *
| $\langle \text{expr} \rangle + \langle \text{expr} \rangle$
| $\langle \text{expr} \rangle * \langle \text{expr} \rangle$
| $\langle \text{variable} \rangle$
| `_let` $\langle \text{variable} \rangle = \langle \text{expr} \rangle `_in` $\langle \text{expr} \rangle$
| `_if` $\langle \text{expr} \rangle$ `_then` $\langle \text{expr} \rangle$ `_else` $\langle \text{expr} \rangle$$

$\langle \text{val} \rangle$ = $\langle \text{number} \rangle$
| $\langle \text{boolean} \rangle$

MSDscript with Booleans

$\langle \text{expr} \rangle$ = $\langle \text{number} \rangle$ **Num**
| $\langle \text{boolean} \rangle$
| $\langle \text{expr} \rangle == \langle \text{expr} \rangle$
| $\langle \text{expr} \rangle + \langle \text{expr} \rangle$
| $\langle \text{expr} \rangle * \langle \text{expr} \rangle$
| $\langle \text{variable} \rangle$
| **_let** $\langle \text{variable} \rangle = \langle \text{expr} \rangle$ **_in** $\langle \text{expr} \rangle$
| **_if** $\langle \text{expr} \rangle$ **_then** $\langle \text{expr} \rangle$ **_else** $\langle \text{expr} \rangle$

$\langle \text{val} \rangle$ = $\langle \text{number} \rangle$ **int**
| $\langle \text{boolean} \rangle$

MSDscript with Booleans

```
⟨expr⟩ = ⟨number⟩ NumExpr
        | ⟨boolean⟩
        | ⟨expr⟩ == ⟨expr⟩
        | ⟨expr⟩ + ⟨expr⟩
        | ⟨expr⟩ * ⟨expr⟩
        | ⟨variable⟩
        | _let ⟨variable⟩ = ⟨expr⟩ _in ⟨expr⟩
        | _if ⟨expr⟩ _then ⟨expr⟩ _else ⟨expr⟩

⟨val⟩ = ⟨number⟩ NumVal
        | ⟨boolean⟩
```


MSDscript with Booleans

```
⟨expr⟩ = ⟨number⟩ NumExpr  
      | ⟨boolean⟩ BoolExpr  
      | ⟨expr⟩ == ⟨expr⟩  
      | ⟨expr⟩ + ⟨expr⟩  
      | ⟨expr⟩ * ⟨expr⟩  
      | ⟨variable⟩  
      | _let ⟨variable⟩ = ⟨expr⟩ _in ⟨expr⟩  
      | _if ⟨expr⟩ _then ⟨expr⟩ _else ⟨expr⟩  
  
⟨val⟩ = ⟨number⟩ NumVal  
      | ⟨boolean⟩ BoolVal
```

MSDscript with Booleans

Expr	$\langle \text{expr} \rangle$	=	$\langle \text{number} \rangle$	NumExpr
			$\langle \text{boolean} \rangle$	BoolExpr
			$\langle \text{expr} \rangle == \langle \text{expr} \rangle$	EqExpr
			$\langle \text{expr} \rangle + \langle \text{expr} \rangle$	AddExpr
			$\langle \text{expr} \rangle * \langle \text{expr} \rangle$	MultExpr
			$\langle \text{variable} \rangle$	VarExpr
			_let $\langle \text{variable} \rangle = \langle \text{expr} \rangle$ _in $\langle \text{expr} \rangle$	LetExpr
			_if $\langle \text{expr} \rangle$ _then $\langle \text{expr} \rangle$ _else $\langle \text{expr} \rangle$	IfExp
Val	$\langle \text{val} \rangle$	=	$\langle \text{number} \rangle$	NumVal
			$\langle \text{boolean} \rangle$	BoolVal

Refactoring MSDscript

Original

`int`

`Expr`

`Num, Add, Mult`

`Var, Let`

`int interp()`

`Expr* subst(...)`

`void print(...), ...`

Refactored

`Val`

`NumVal, BoolVal`

`Expr* to_expr(), ...`

`Expr`

`NumExpr, AddExpr, MultExpr`

`VarExpr, LetExpr`

`BoolExpr, EqExpr, IfExpr`

`Val* interp()`

`Expr* subst(...)`

`void print(...), ...`

Evaluation

1 + 2
➡ 3

```
CHECK( (new AddExpr(new NumExpr(1), new NumExpr(2))) ->interp()  
      ->equals(new NumVal(3)) );
```

```
CHECK( parse_str("1 + 2") ->interp()  
      ->equals(new NumVal(3)) );
```

```
CHECK( parse_str("1 + 2") ->interp() ->to_string() == "3" );
```

```
static std::string run(std::string s) {  
    return parse_str(s) ->interp() ->to_string();  
}  
CHECK( run("1 + 2") == "3" );
```

Evaluation

1 == 2

➡ `_false`

```
CHECK( (new EqExpr(new NumExpr(1), new NumExpr(2))) ->interp()  
->equals(new BoolVal(false)) );
```

```
CHECK( parse_str("1 == 2") ->interp()  
->equals(new BoolVal(false)) );
```

```
CHECK( parse_str("1 == 2") ->interp() ->to_string() == "_false" );
```

```
static std::string run(std::string s) {  
    return parse_str(s) ->interp() ->to_string();  
}  
CHECK( run("1 == 2") == "_false" );
```

Evaluation

1 == 2

➡ `_false`

```
CHECK( (new EqExpr(new NumExpr(1), new NumExpr(2))) ->interp()  
      ->equals(new BoolVal(false)) );
```

```
CHECK( parse_str("1 == 2") ->interp()  
      ->equals(new BoolVal(false)) );
```

```
CHECK( parse_str("1 == 2") ->interp() ->to_string() == "_false" );
```

```
static std::string run(std::string s) {  
    return parse_str(s) ->interp() ->to_string();  
}  
CHECK( run("1 == 2") == "_false" );
```

Parsing with Conditions and Comparisons

$\langle \text{expr} \rangle$ = $\langle \text{comparg} \rangle$
| $\langle \text{comparg} \rangle == \langle \text{expr} \rangle$

$\langle \text{comparg} \rangle$ = $\langle \text{addend} \rangle$
| $\langle \text{addend} \rangle + \langle \text{comparg} \rangle$

$\langle \text{addend} \rangle$ = $\langle \text{multicand} \rangle$
| $\langle \text{multicand} \rangle * \langle \text{addend} \rangle$

$\langle \text{multicand} \rangle$ = $\langle \text{number} \rangle$
| $(\langle \text{expr} \rangle)$
| $\langle \text{variable} \rangle$
| `_let` $\langle \text{variable} \rangle = \langle \text{expr} \rangle$ `_in` $\langle \text{expr} \rangle$
| `_true`
| `_false`
| `_if` $\langle \text{expr} \rangle$ `_then` $\langle \text{expr} \rangle$ `_else` $\langle \text{expr} \rangle$

Parsing with Conditions and Comparisons

```
parse_expr      <expr>    = <comparg>
                  | <comparg> == <expr>

parse_comparg    <comparg> = <addend>
                  | <addend> + <comparg>

parse_addend     <addend>  = <multicand>
                  | <multicand> * <addend>

parse_multicand  <multicand> = <number>
                  | ( <expr> )
                  | <variable>
                  | _let <variable> = <expr> _in <expr>
                  | _true
                  | _false
                  | _if <expr> _then <expr> _else <expr>
```


Parsing with Conditions and Comparisons

	$\langle \text{expr} \rangle$ = $\langle \text{comparg} \rangle$ $\langle \text{comparg} \rangle == \langle \text{expr} \rangle$
	$\langle \text{comparg} \rangle$ = $\langle \text{addend} \rangle$ $\langle \text{addend} \rangle + \langle \text{comparg} \rangle$
	$\langle \text{addend} \rangle$ = $\langle \text{multicand} \rangle$ $\langle \text{multicand} \rangle * \langle \text{addend} \rangle$
<pre> parse_multicand() { if (isdigit(next_ch)) parse_number() else if (next_ch == '(') parse_expr() else if (isalpha(next_ch)) parse_variable() else if (next_ch == '_') { kw = parse_keyword() if (kw == "_let") parse_let() else if (kw == "_false") ... else if (kw == "_true") ... else if (kw == "_if") parse_if() } } </pre>	$\langle \text{multicand} \rangle$ = $\langle \text{number} \rangle$ $(\langle \text{expr} \rangle)$ $\langle \text{variable} \rangle$ $_let \langle \text{variable} \rangle = \langle \text{expr} \rangle _in \langle \text{expr} \rangle$ $_true$ $_false$ $_if \langle \text{expr} \rangle _then \langle \text{expr} \rangle _else \langle \text{expr} \rangle$

Evaluation

1 + 2

➡ 3

```
CHECK( (new AddExpr(new NumExpr(1), new NumExpr(2))) ->interp()  
      ->equals(new NumVal(3)) );
```

```
Val *AddExpr::interp() {  
}
```

Evaluation

1 + 2
➡ 3

```
CHECK( (new AddExpr(new NumExpr(1), new NumExpr(2))) ->interp()  
      ->equals(new NumVal(3)) );
```

```
Val *AddExpr::interp() {  
    .... lhs    ....  
    .... rhs    ....  
}
```

Evaluation

1 + 2
➡ 3

```
CHECK( (new AddExpr(new NumExpr(1), new NumExpr(2))) ->interp()  
      ->equals(new NumVal(3)) );
```

```
Val *AddExpr::interp() {  
    .... lhs->interp() ....  
    .... rhs->interp() ....  
}
```

When you have an **Expr**, **interp** it

(3 * 4) + 1 1 + (_if _true _then 1 _else 2)

Evaluation

1 + 2

➡ 3

```
CHECK( (new AddExpr(new NumExpr(1), new NumExpr(2))) ->interp()  
      ->equals(new NumVal(3)) );
```

```
Val *AddExpr::interp() {  
    .... lhs->interp() ....  
    .... rhs->interp() ....  
}
```

```
Val *NumExpr::interp() {  
    return new NumVal(rep);  
}
```

Evaluation

1 + 2

➡ 3

```
CHECK( (new AddExpr(new NumExpr(1), new NumExpr(2))) ->interp()  
->equals(new NumVal(3)) );
```

```
Val *AddExpr::interp()  
.... lhs->interp()  
.... rhs->interp()  
}
```

```
class NumExpr : public Expr {  
    int rep;  
    NumExpr(int rep) {  
        this->rep = rep;  
    }  
};
```

```
Val *NumExpr::interp() {  
    return new NumVal(rep);  
}
```

Evaluation

1 + 2
➡ 3

```
CHECK( (new AddExpr(new NumExpr(1), new NumExpr(2))) ->interp()  
      ->equals(new NumVal(3)) );
```

```
Val *AddExpr::interp() {  
    return lhs->interp()  
        ->add_to(rhs->interp());  
}
```

Object-oriented style: let a **Val** decide about operations

Evaluation

1 + 2
➡ 3

```
CHECK( (new AddExpr(new NumExpr(1), new NumExpr(2))) ->interp()  
      ->equals(new NumVal(3)) );
```

```
Val *AddExpr::interp() {  
    return lhs->interp()  
        ->add_to(rhs->interp());  
}
```

```
Val *NumVal::add_to(Val *other_val) {  
    NumVal *other_num = dynamic_cast<NumVal*>(other_val);  
    if (other_num == NULL) throw std::runtime_error("add of non-number");  
    return new NumVal(rep + other_num->rep);  
}
```


Evaluation

1 + 2
➡ 3

```
CHECK( (new AddExpr(new NumExpr(1), new NumExpr(2))) ->interp()  
      ->equals(new NumVal(3)) );
```

```
Val *AddExpr::interp() {  
    return lhs->interp()  
        ->add_to(rhs->interp());  
}
```

Allowed because only **NumVal** makes sense

```
Val *NumVal::add_to(Val *other_val) {  
    NumVal *other_num = dynamic_cast<NumVal*>(other_val);  
    if (other_num == NULL) throw std::runtime_error("add of non-number");  
    return new NumVal(rep + other_num->rep);  
}
```

Evaluation

1 + 2
➡ 3

```
CHECK( (new AddExpr(new NumExpr(1), new NumExpr(2))) ->interp()  
->equals(new NumVal(3)) );
```

```
Val *AddExpr::interp() {  
    return lhs->interp()  
        ->add_to(rhs->interp());  
}
```

```
Val *BoolVal::add_to(Val *other_val) {  
    throw std::runtime_error("add of non-number");  
}
```

Evaluation

```
_let x = 2+3  
_in x*x
```

```
CHECK( (new LetExpr("x",  
                    new AddExpr(new NumExpr(2), new NumExpr(3)),  
                    new MultExpr(new VarExpr("x"), new VarExpr("x"))))  
->interp()  
->equals(new NumVal(25)) );
```

```
Val *LetExpr::interp() {  
}
```

Evaluation

```
_let x = 2+3  
_in x*x
```

```
CHECK( (new LetExpr("x",  
                    new AddExpr(new NumExpr(2), new NumExpr(3)),  
                    new MultExpr(new VarExpr("x"), new VarExpr("x"))))  
->interp()  
->equals(new NumVal(25)) );
```

```
Val *LetExpr::interp() {  
    .... lhs ....  
    .... rhs ....  
    .... body ....  
}
```

Evaluation

```
_let x = 2+3  
_in x*x
```

```
CHECK( (new LetExpr("x",  
                    new AddExpr(new NumExpr(2), new NumExpr(3)),  
                    new MultExpr(new VarExpr("x"), new VarExpr("x"))))  
->interp()  
->equals(new NumVal(25)) );
```

```
Val *LetExpr::interp() {  
    .... lhs ....  
    .... rhs->interp() ....  
    .... body->interp() ....  
}
```

Evaluation

```
_let x = 2+3  
_in x*x
```

```
CHECK( (new LetExpr("x",  
                    new AddExpr(new NumExpr(2), new NumExpr(3)),  
                    new MultExpr(new VarExpr("x"), new VarExpr("x"))))  
->interp()  
->equals(new NumVal(25)) );
```

```
Val *LetExpr::interp() {  
    .... lhs ....  
    .... rhs->interp() ....  
    .... body->subst( ... )->interp() ....  
}
```

Evaluation

```
_let x = 2+3  
_in x*x
```

```
CHECK( (new LetExpr("x",  
                    new AddExpr(new NumExpr(2), new NumExpr(3)),  
                    new MultExpr(new VarExpr("x"), new VarExpr("x"))))  
->interp()  
->equals(new NumVal(25)) );
```

```
Val *LetExpr::interp() {  
  
    .... rhs->interp() ....  
    .... body->subst(lhs, ...) ->interp() ....  
}
```

Evaluation

```
_let x = 2+3  
_in x*x
```

```
CHECK( (new LetExpr("x",  
                    new AddExpr(new NumExpr(2), new NumExpr(3)),  
                    new MultExpr(new VarExpr("x"), new VarExpr("x"))))  
->interp()  
->equals(new NumVal(25)) );
```

```
Val *LetExpr::interp() {  
  
    Val *rhs_val = rhs->interp();  
    .... body->subst(lhs, ... rhs_val ...)->interp()  
}
```


Evaluation

```
_let x = 2+3  
_in x*x
```

```
class Val {  
    virtual Expr *to_expr() = 0;  
}
```

```
CHECK( (new LetExpr("x",  
                    new AddExpr(new NumExpr(2), new NumExpr(3)),  
                    new MultExpr(new VarExpr("x"), new VarExpr("x"))))  
->interp()  
->equals(new NumVal(25)) );
```

```
Val *LetExpr::interp() {  
  
    Val *rhs_val = rhs->interp();  
    .... body->subst(lhs, rhs_val->to_expr())->interp()  
}
```

Evaluation

```
_let x = 2+3  
_in x*x
```

```
CHECK( (new LetExpr("x",  
                    new AddExpr(new NumExpr(2), new NumExpr(3)),  
                    new MultExpr(new VarExpr("x"), new VarExpr("x"))))  
->interp()  
->equals(new NumVal(25)) );
```

```
Val *LetExpr::interp() {  
  
    Val *rhs_val = rhs->interp();  
    return body->subst(lhs, rhs_val->to_expr())->interp();  
}
```

Conditional Evaluation

```
_if _true  
_then 1  
_else 2
```

```
CHECK( (new IfExpr(new BoolExpr(true),  
                    new NumExpr(1),  
                    new NumExpr(2))) ->interp()  
->equals(new NumVal(1)) );
```

```
Val *IfExpr::interp() {  
}
```

Conditional Evaluation

```
_if _true  
_then 1  
_else 2
```

```
CHECK( (new IfExpr(new BoolExpr(true),  
                    new NumExpr(1),  
                    new NumExpr(2))) ->interp()  
      ->equals(new NumVal(1)) );
```

```
Val *IfExpr::interp() {  
    .... test_part ....  
    .... then_part ....  
    .... else_part ....  
  
}
```

Conditional Evaluation

```
_if _true  
_then 1  
_else 2
```

```
CHECK( (new IfExpr(new BoolExpr(true),  
                    new NumExpr(1),  
                    new NumExpr(2))) ->interp()  
      ->equals(new NumVal(1)) );
```

```
Val *IfExpr::interp() {  
    .... test_part->interp() ....  
    .... then_part->interp() ....  
    .... else_part->interp() ....  
  
}
```

Conditional Evaluation

```
_if _true  
_then 1  
_else 2
```

```
CHECK( (new IfExpr(new BoolExpr(true),  
                    new NumExpr(1),  
                    new NumExpr(2))) ->interp()  
      ->equals(new NumVal(1)) );
```

```
Val *IfExpr::interp() {  
    .... test_part->interp()->is_true() ....  
    .... then_part->interp() ....  
    .... else_part->interp() ....  
  
}
```

Conditional Evaluation

```
_if _true  
_then 1  
_else 2
```

```
class Val {  
    virtual bool is_true() = 0;  
}
```

```
CHECK( (new IfExpr(new BoolExpr(true),  
                    new NumExpr(1),  
                    new NumExpr(2))) ->interp()  
      ->equals(new NumVal(1)) );
```

```
Val *IfExpr::interp() {  
    .... test_part->interp()->is_true() ....  
    .... then_part->interp() ....  
    .... else_part->interp() ....  
  
}
```

Conditional Evaluation

```
_if _true  
_then 1  
_else 2
```

```
CHECK( (new IfExpr(new BoolExpr(true),  
                    new NumExpr(1),  
                    new NumExpr(2))) ->interp()  
      ->equals(new NumVal(1)) );
```

```
Val *IfExpr::interp() {  
    if (test_part->interp()->is_true())  
        return then_part->interp();  
    else  
        return else_part->interp();  
}
```